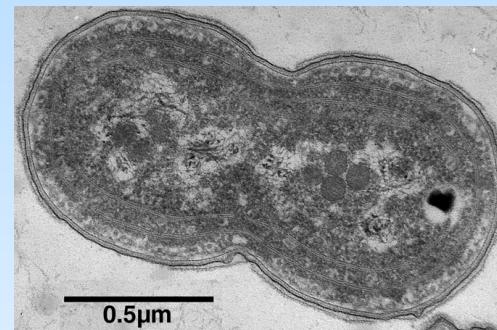
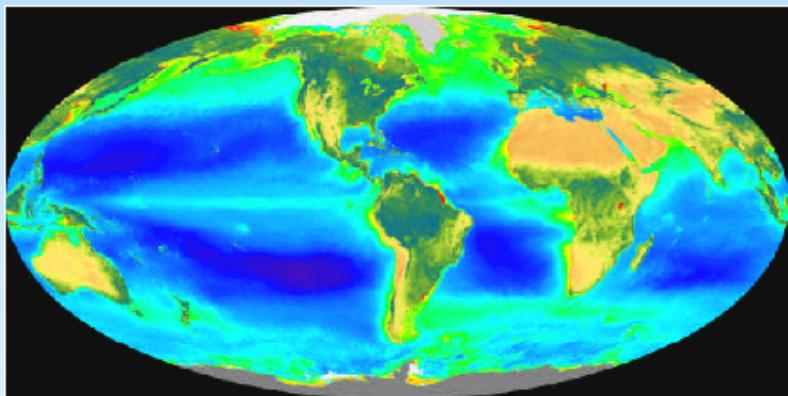


Phytoplankton-Zooplankton Modeling

Scott Doney

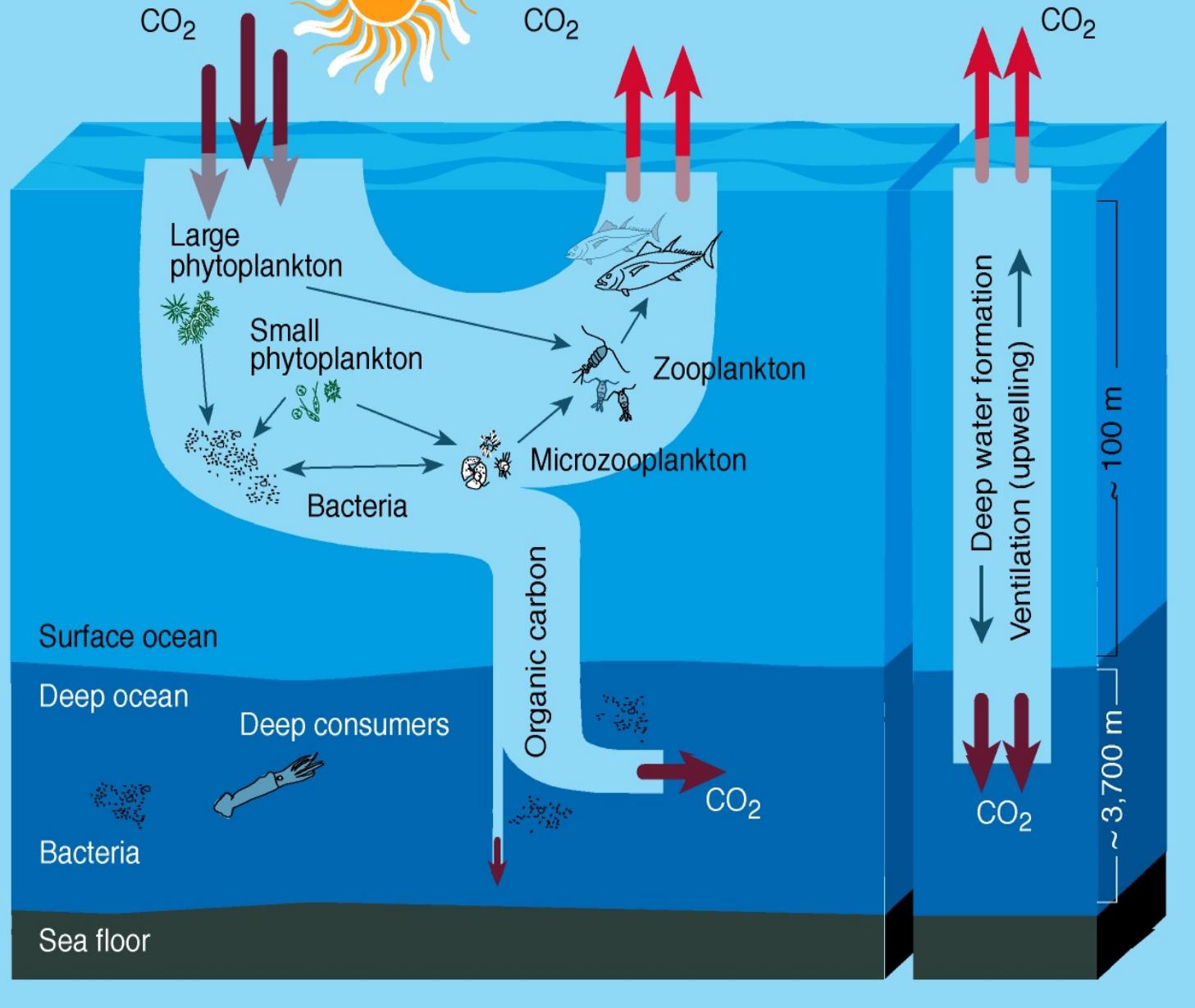
Woods Hole Oceanographic Institution
NCAR ASP Colloquium 2013



Supported by:



Marine Ecology & Biogeochemistry



Model Elements Depend on Science Questions

Carbon Cycle & Biogeochemistry

Ecology & Food-webs

- Phytoplankton, zooplankton, bacteria, ...
- Biological interactions (growth, predation, competition, disease, vertical migration, ...)



Modeling Methods for Marine Science

David M. Glover, William J. Jenkins and Scott C. Doney



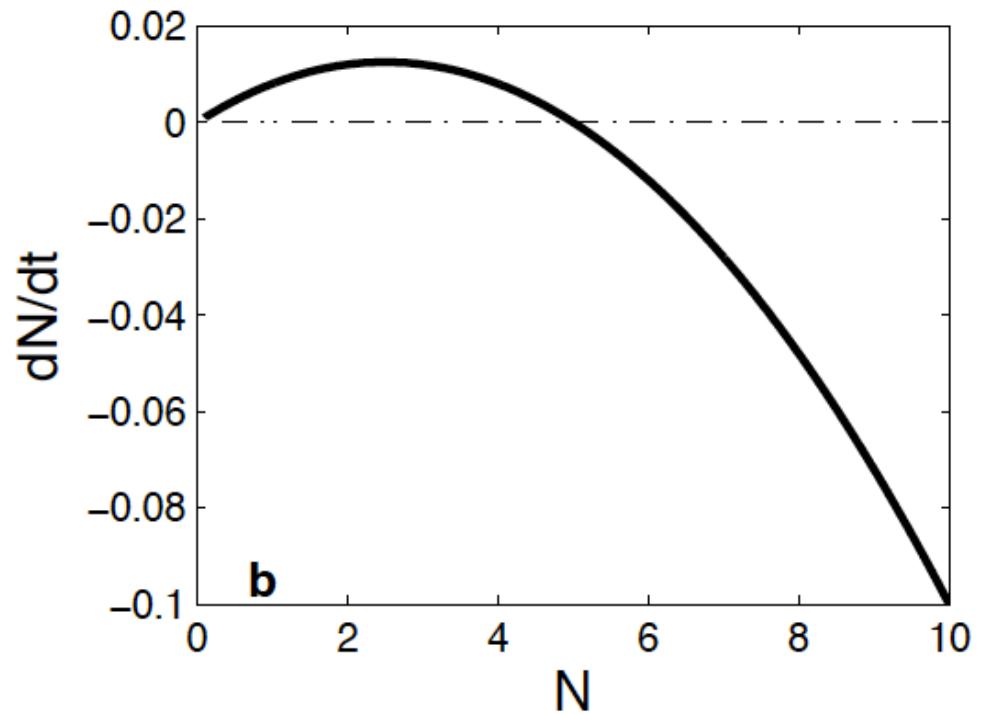
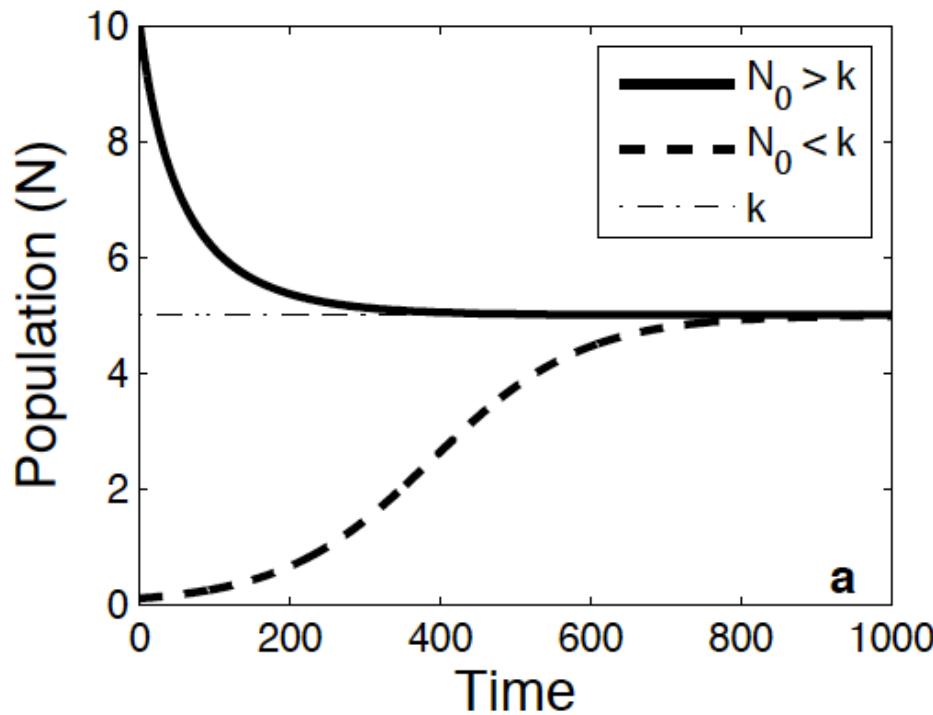
Glover, D.M., W.J. Jenkins,
and S.C. Doney, 2011:
Modeling Methods for Marine
Science
Cambridge University Press
Cambridge, UK, 592 pp.
www.cambridge.org/glover
ISBN-13: 9780521867832



Simple Population Model

Logistic model

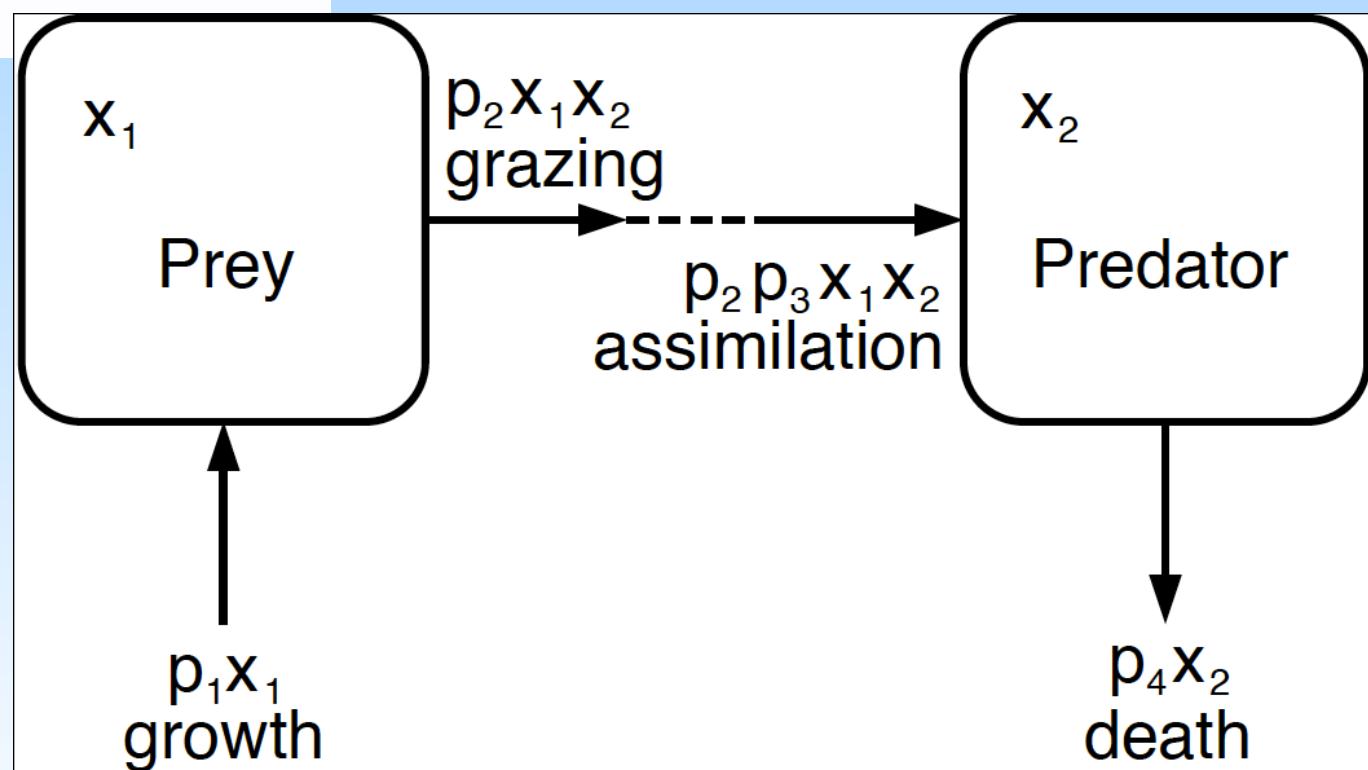
$$\frac{dN}{dt} = \mu \left(1 - \frac{N}{k}\right) N$$



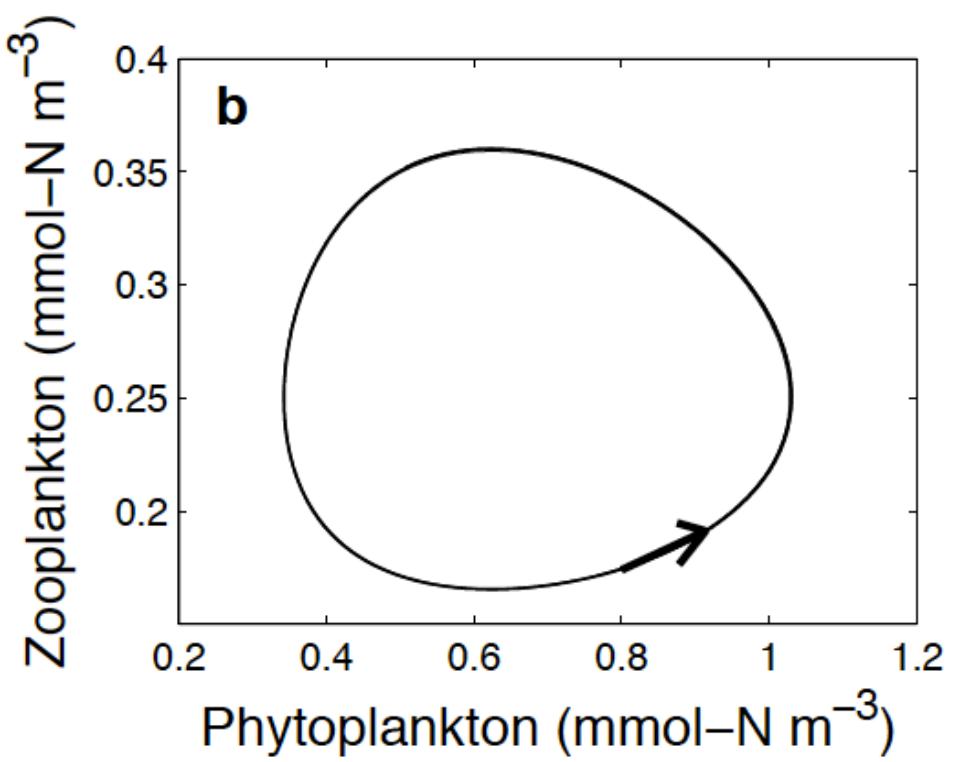
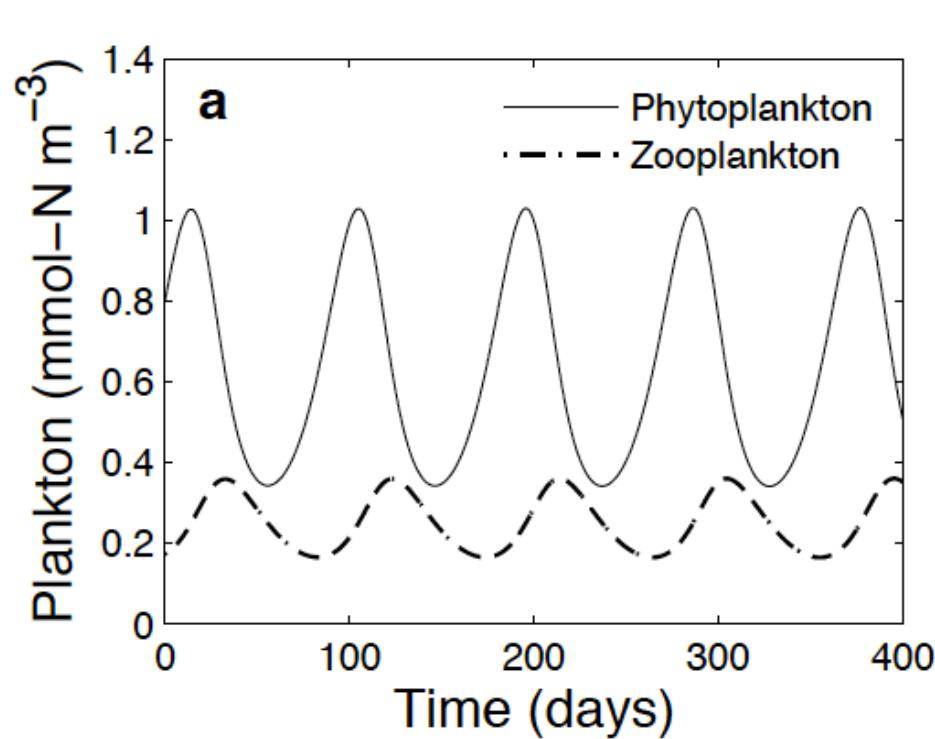
$$\frac{dP}{dt} = \mu P - g P Z$$

$$\frac{dZ}{dt} = \gamma g P Z - m Z$$

Lotka-Volterra Predator-Prey Model



Lotka-Volterra Predator-Prey Model



Simple NPZ Model

$$\frac{dP}{dt} = \mu_0 \left(\frac{N}{k_N + N} \right) \left(1 - e^{\alpha E / \mu_0} \right) P - g \left(\frac{P}{k_P + P} \right) Z - m_P P$$

Nutrient limitation Light limitation Grazing Mortality

$$\frac{dZ}{dt} = ag \left(\frac{P}{k_P + P} \right) Z - m_Z Z$$

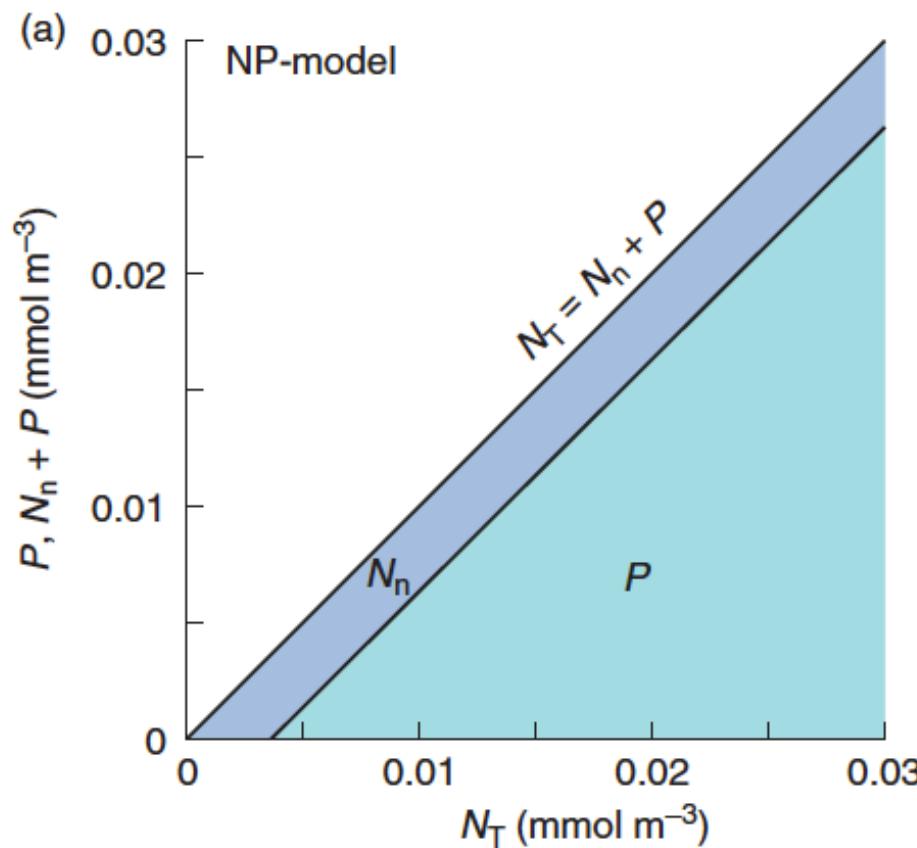
$$\frac{dN}{dt} = -\mu_0 \left(\frac{N}{k_N + N} \right) \left(1 - e^{\alpha E / \mu_0} \right) P + (1 - a)g \left(\frac{P}{k_P + P} \right) Z + m_P P + m_Z Z$$

- Three coupled ordinary differential equations
- Mass conservation



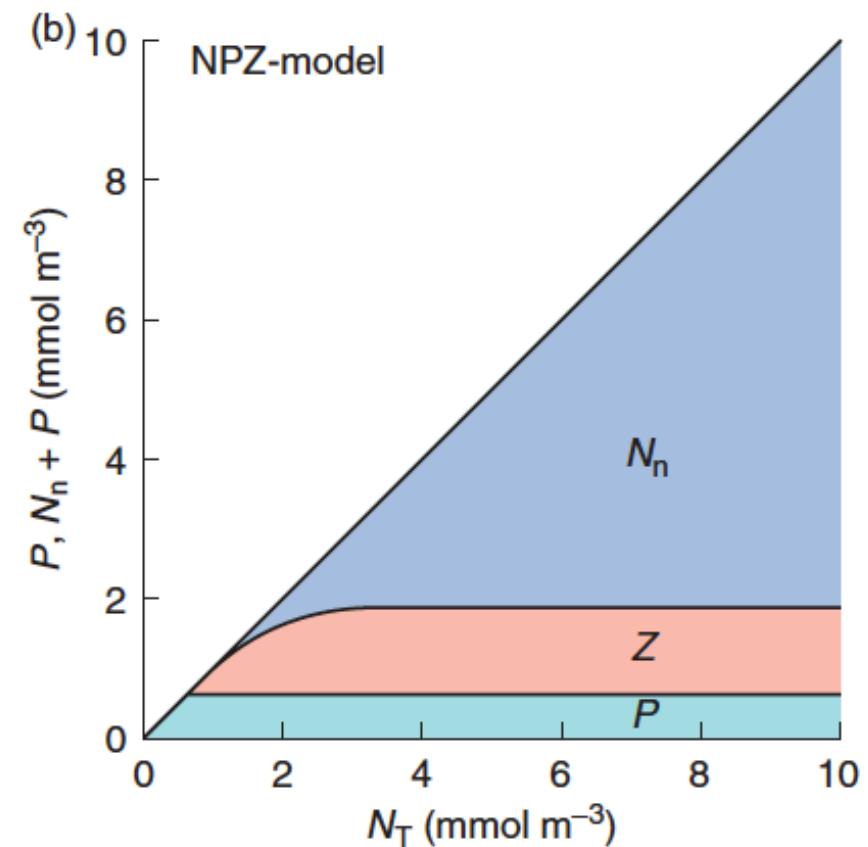
Zooplankton & Nutrient Partitioning

Steady-state (supply=export)



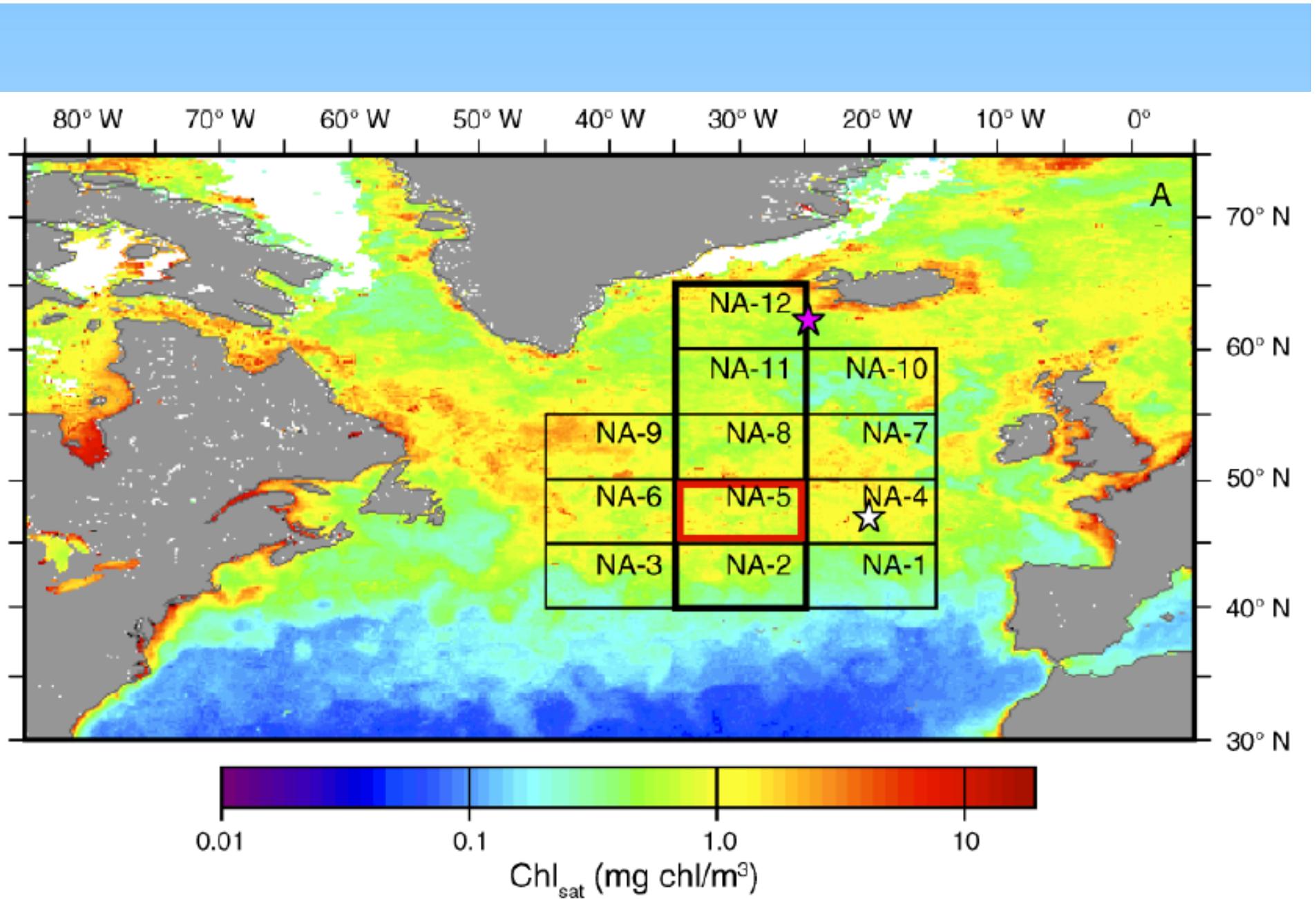
N supply →

$$\gamma m_P P = Supply$$

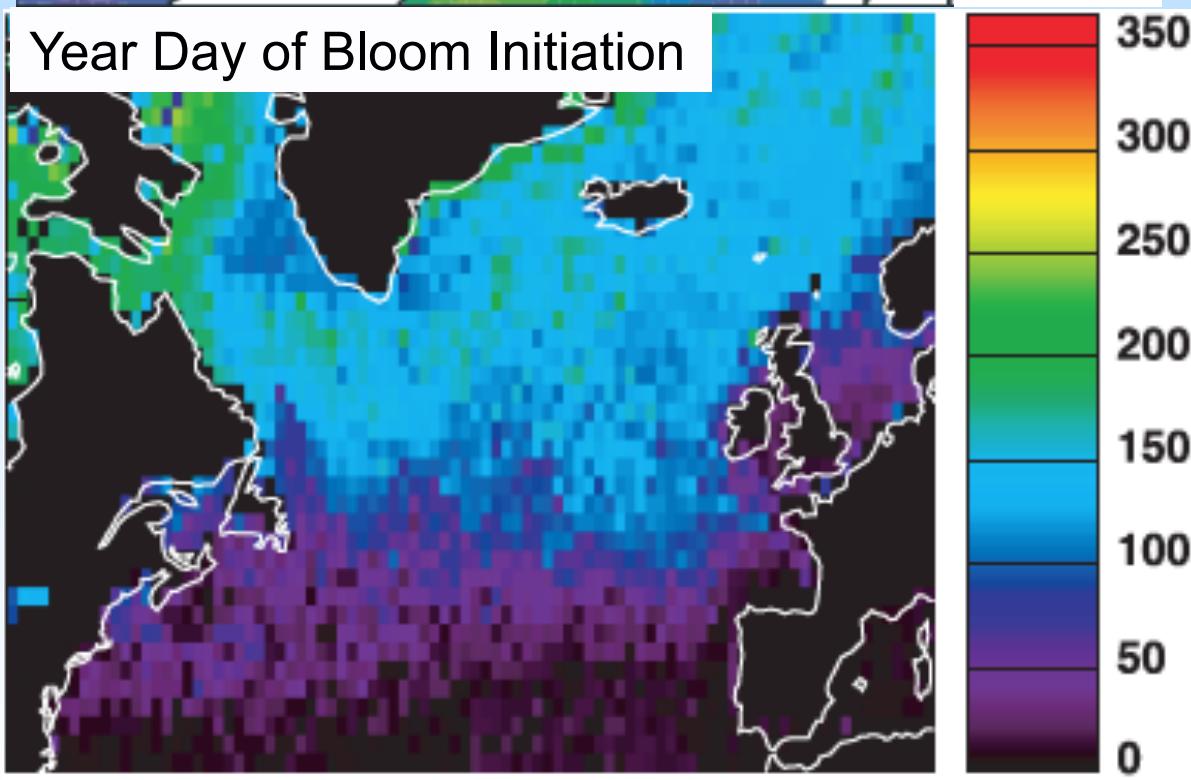
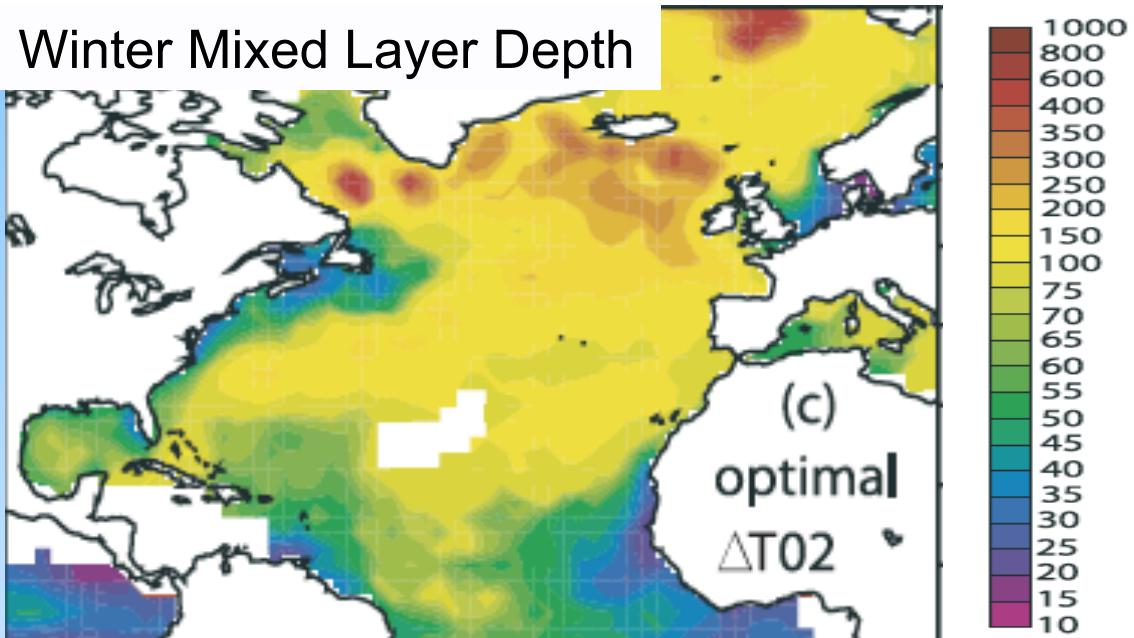


N supply →





Seasonal Progression of Bloom

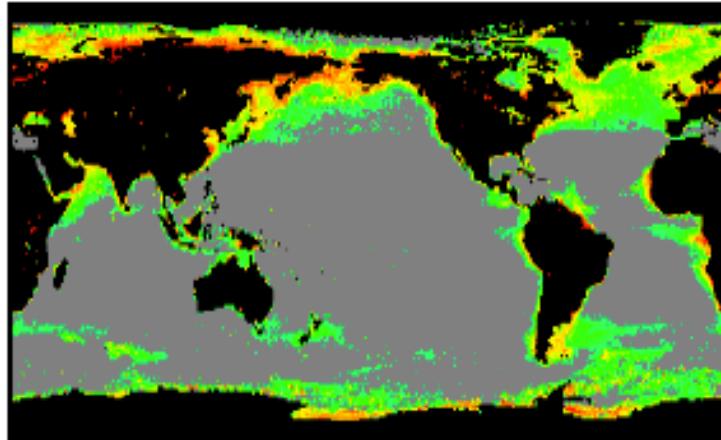


Siegel et al.
Science 2000

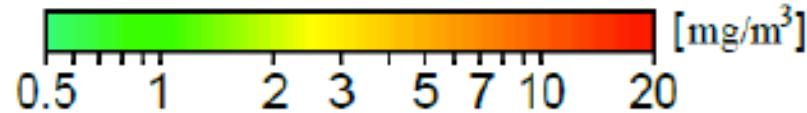
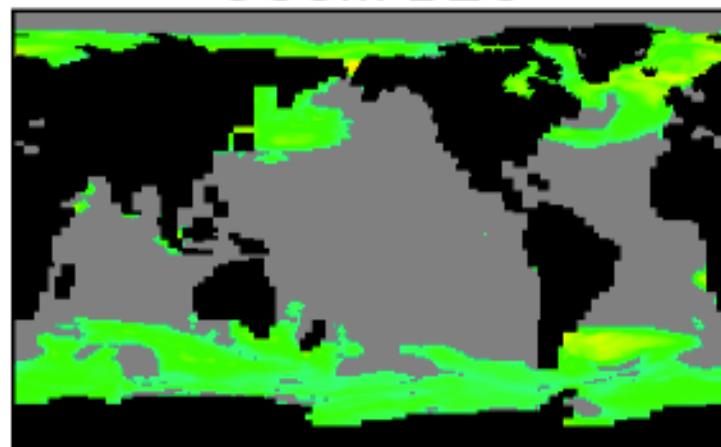


(a) Maximum Chl-a Conc.

SeaWiFS

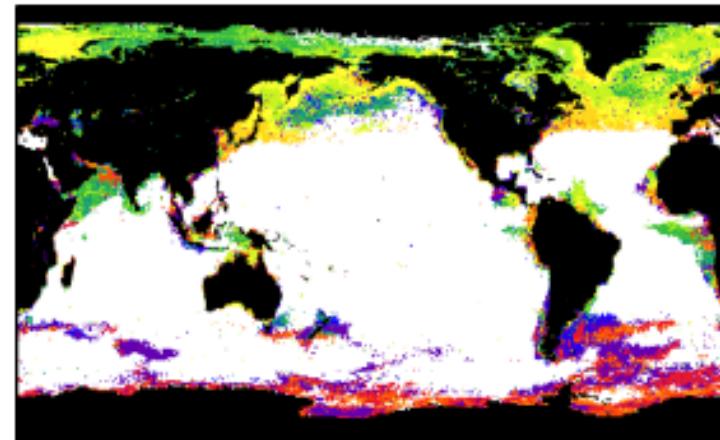


CCSM-BEC

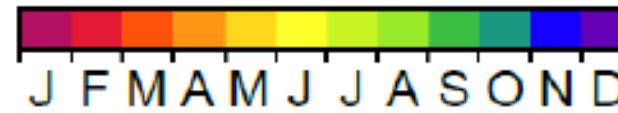
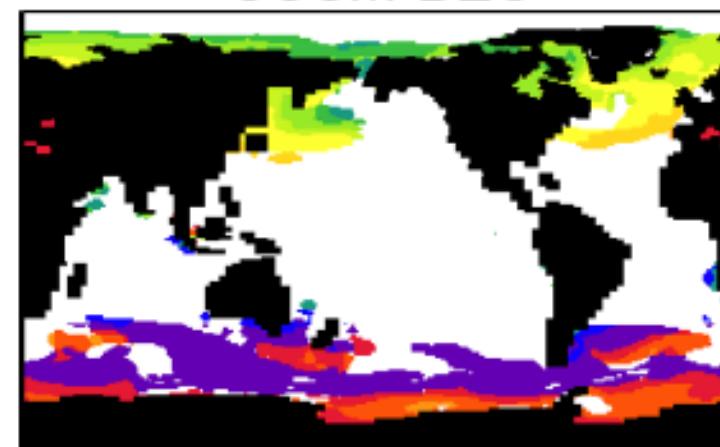


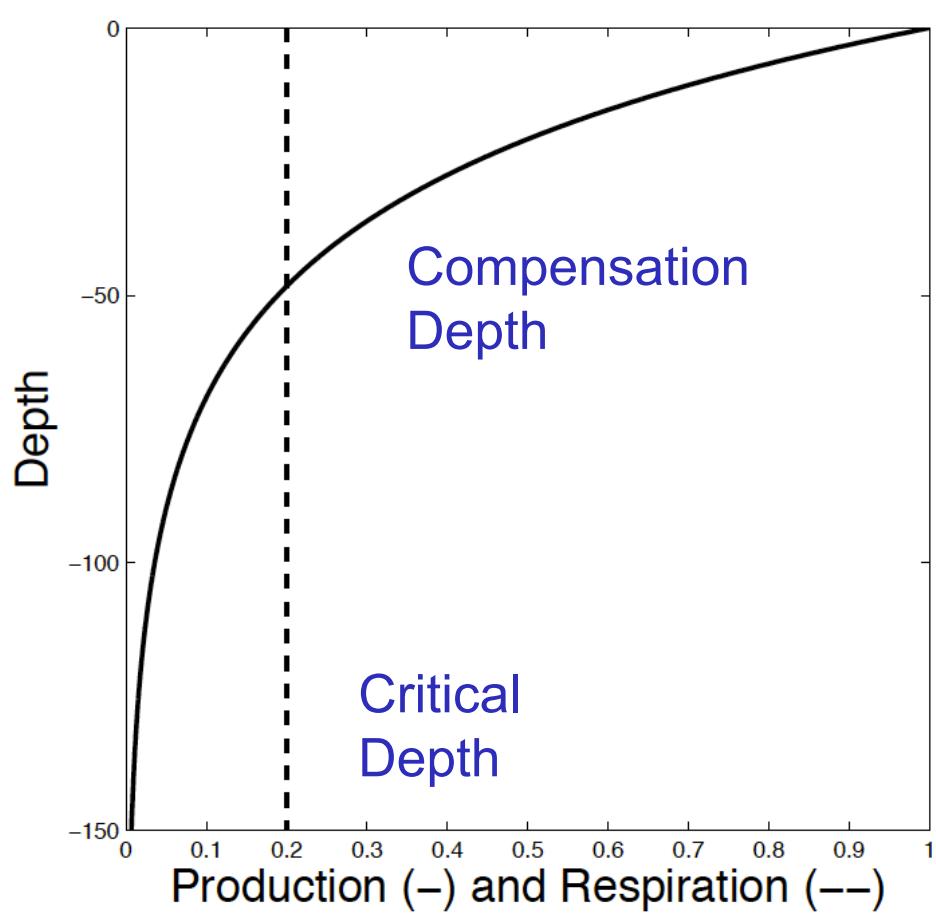
(b) Timing of Max. Chl-a Conc.

SeaWiFS



CCSM-BEC





Bloom occurs when either light increases or mixed layer shoals so that $Z < Z_{cr}$

Sverdrup Bloom Model

Light

$$I(z) = I_0 e^{-kz}$$

Production

$$PP(z) = \alpha I_0 e^{-kz}$$

Compensation Depth

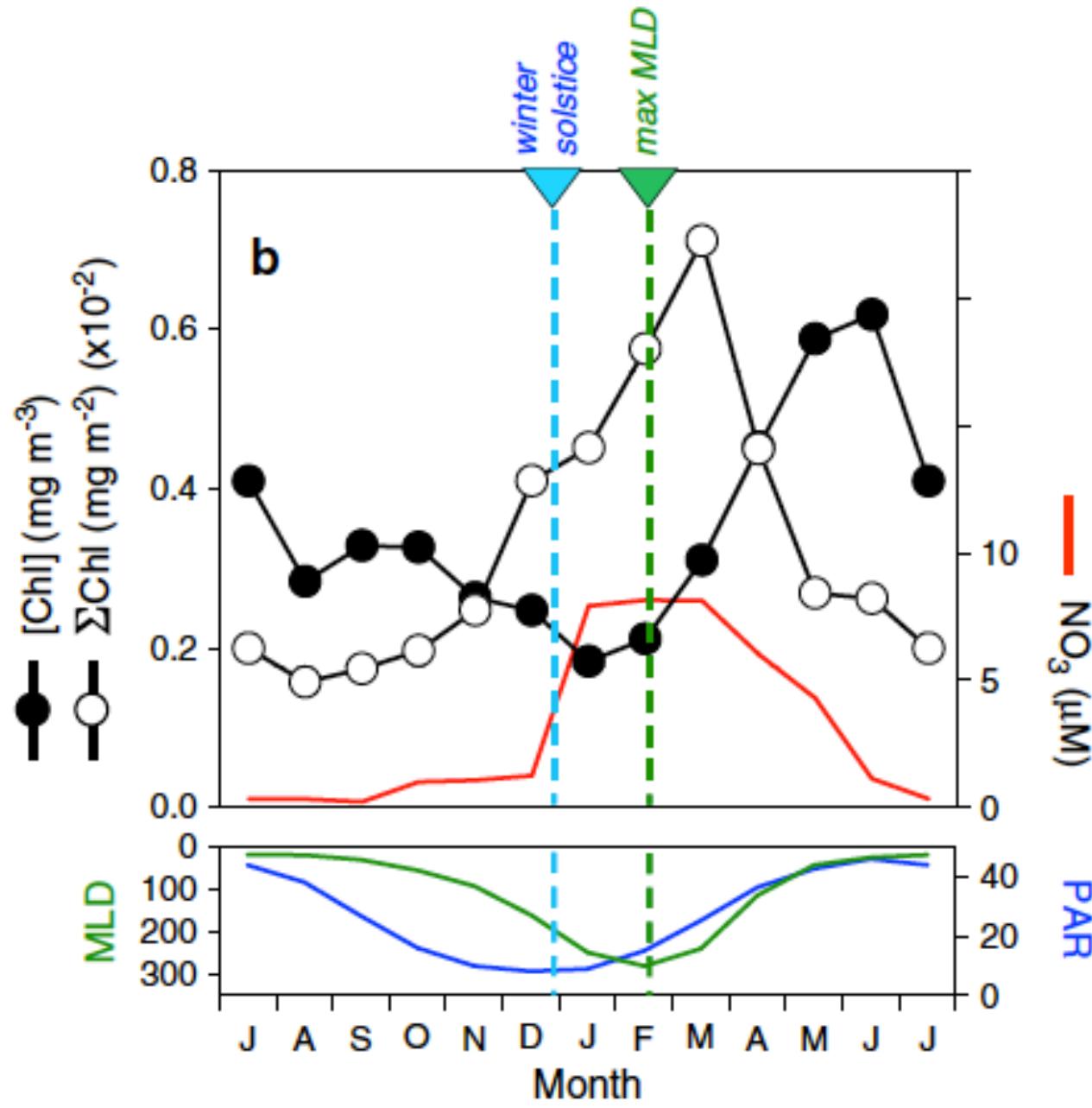
$$PP(z_{comp}) = R(z_{comp})$$

Critical Depth

$$\int_0^{z_{cr}} PP dz = \int_0^{z_{cr}} R dz$$



Ecological Disturbance & Recovery



Behrenfeld et al.
Global Biogeochem.
Cycles 2013

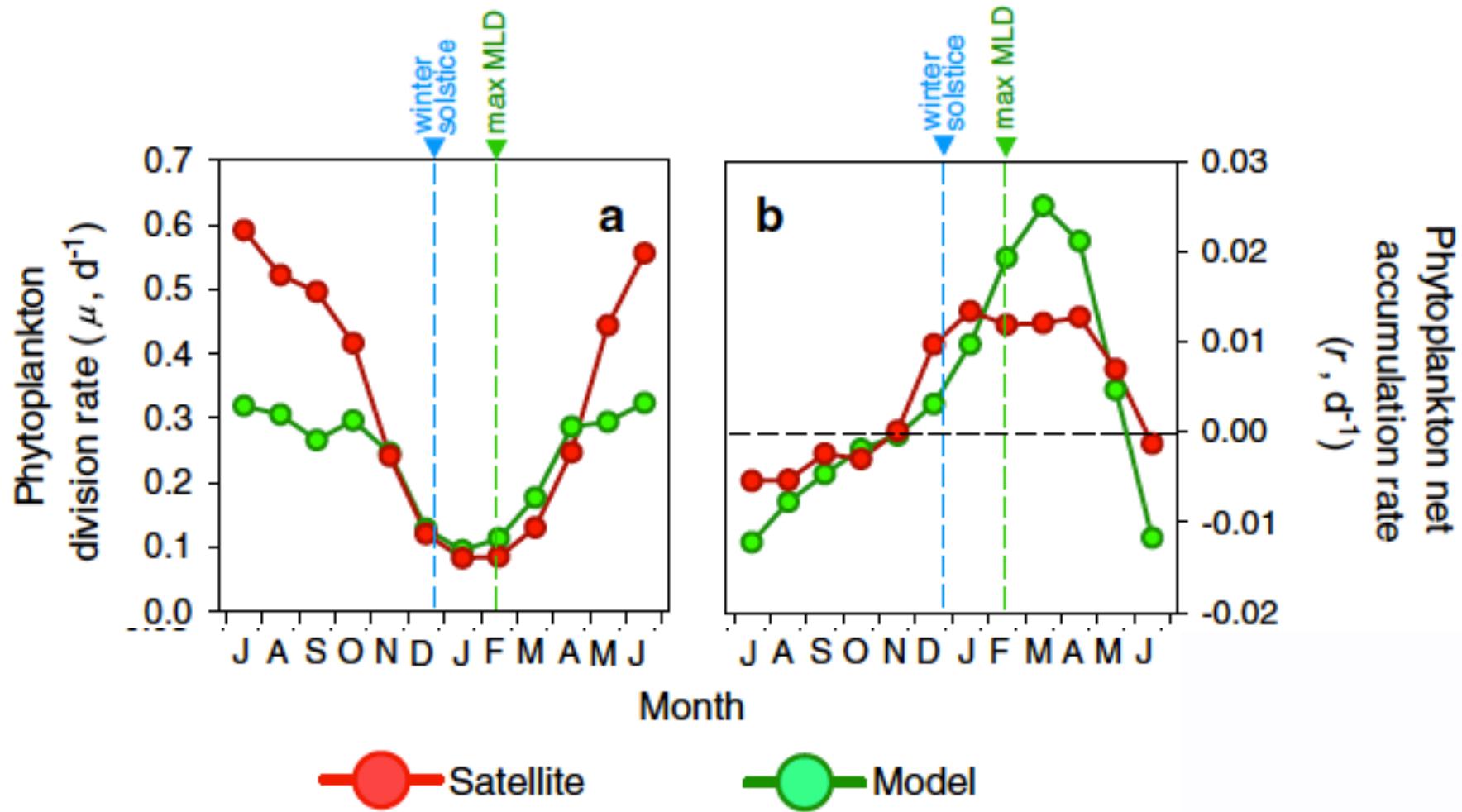


Net
specific
growth
(d^{-1})

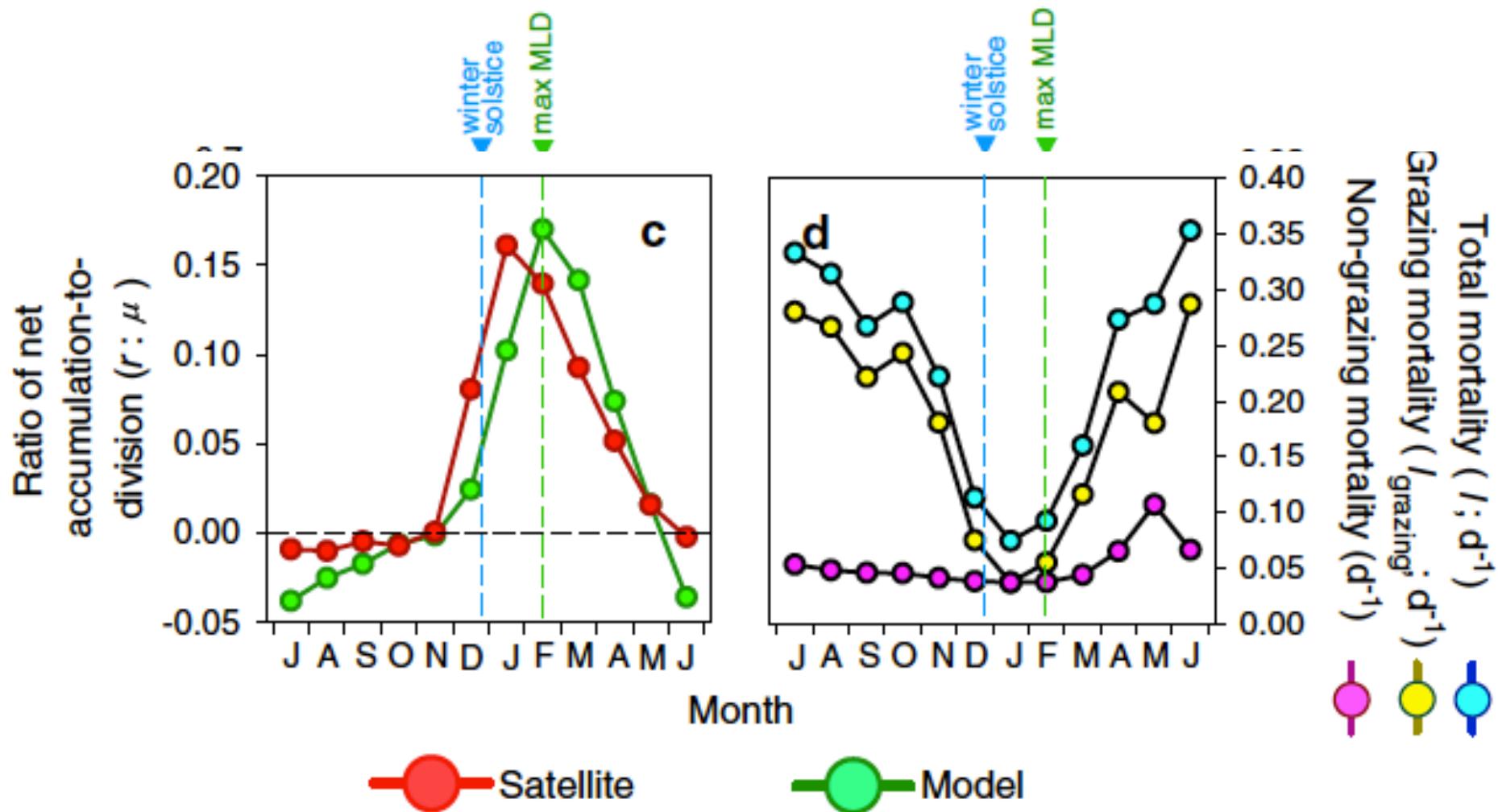
$$r = \frac{1}{\Delta\tau} \ln\left(\frac{C_1}{C_0}\right)$$

$$r = \mu - g - s - p - f$$

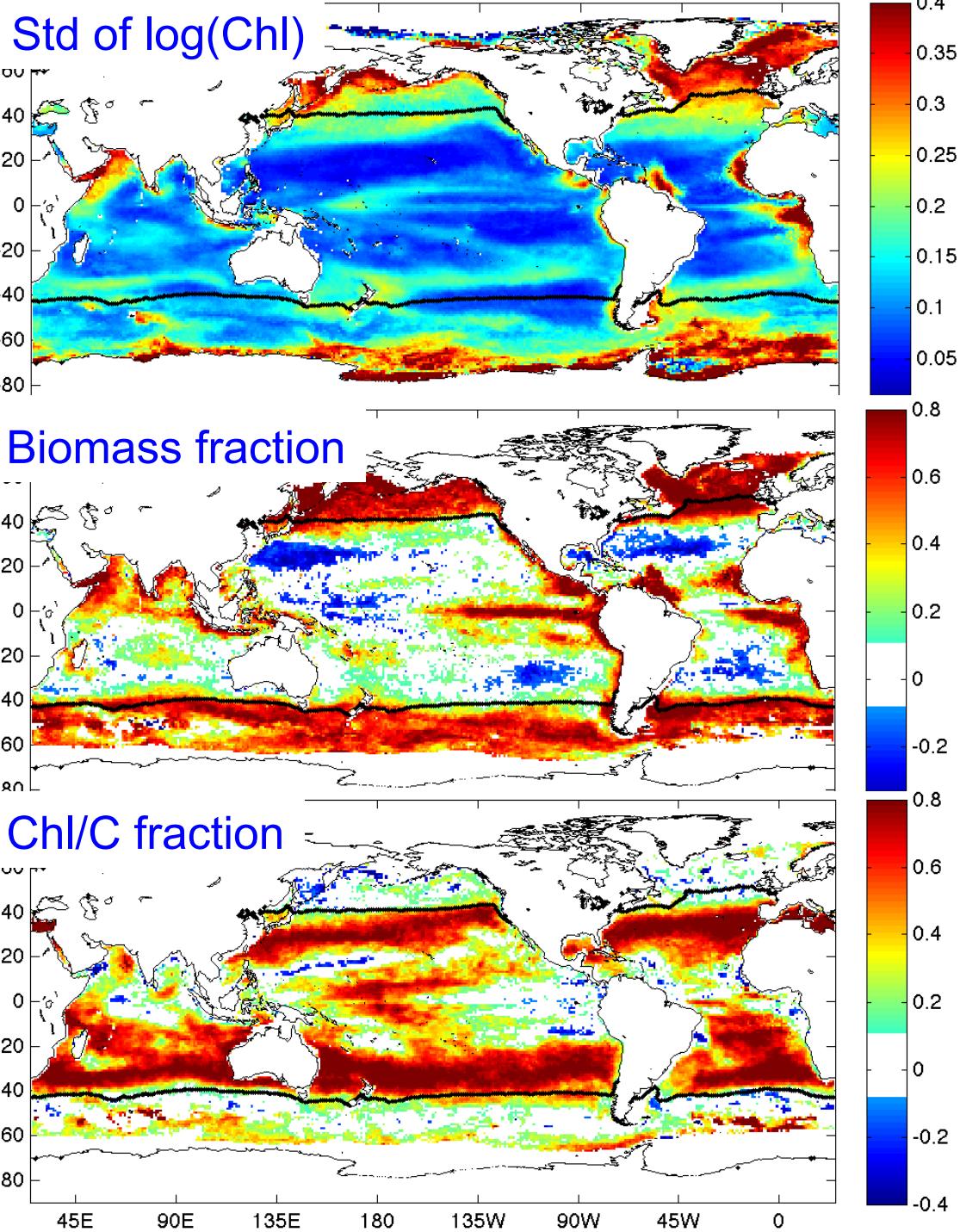
growth – grazing ~ 0



Growth and Loss Terms

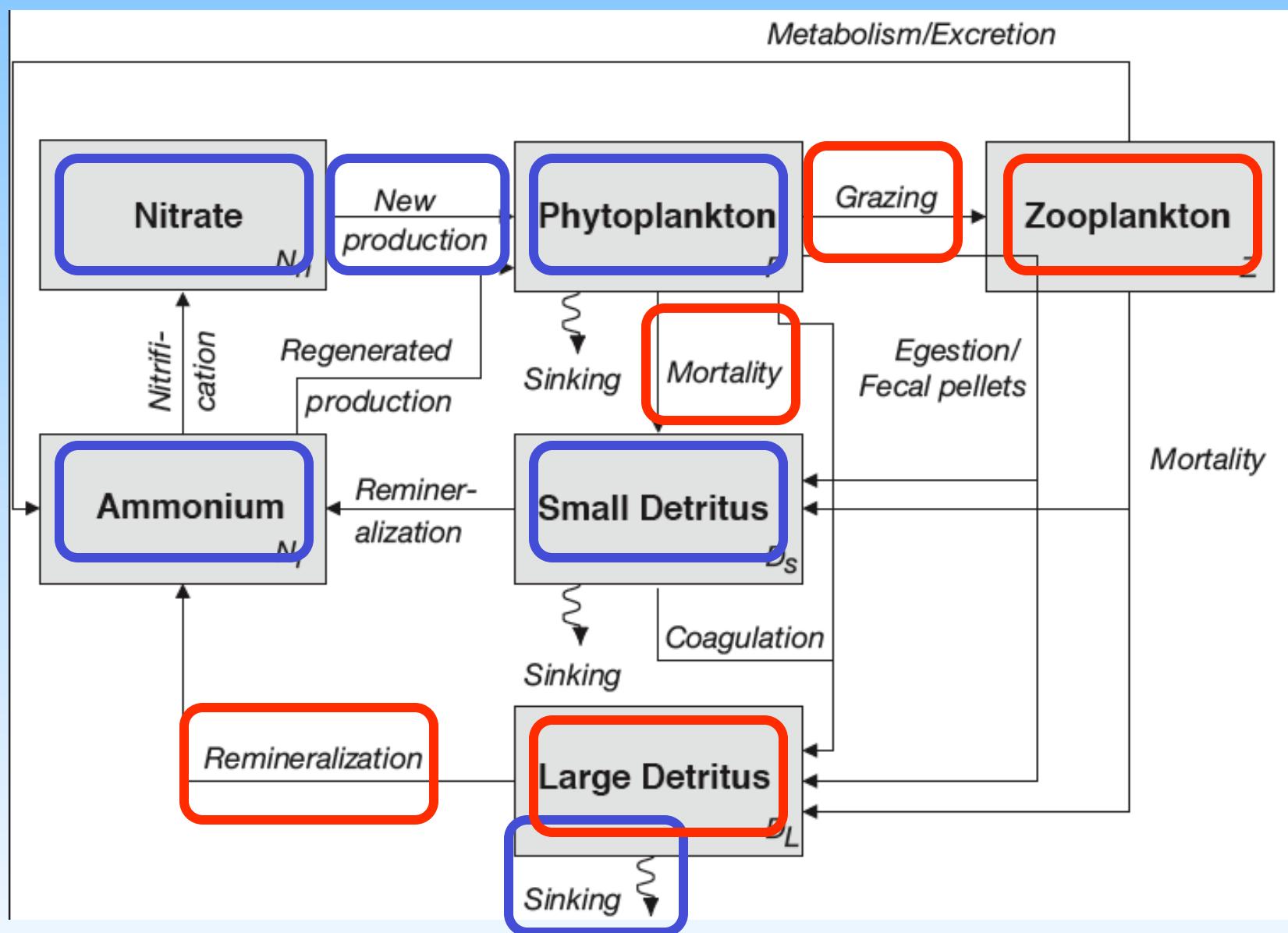


Chlorophyll Variability: Biomass vs. Photoacclimation



Siegel et al.
Remote Sensing Environ.
2013





“Stocks” versus “Rates”
 C
 dC/dt

Estimated from data
 Unknowns



How do you estimate parameters and functional forms?

↳ Laboratory & field incubations

- Photosynthesis-light curves; nutrient uptake curves
- elemental stoichiometry

Comparative analysis

- allometric relationships

Tuned or optimized against field data

- mismatch between parameters and data
- cross-site comparison

Previous models

