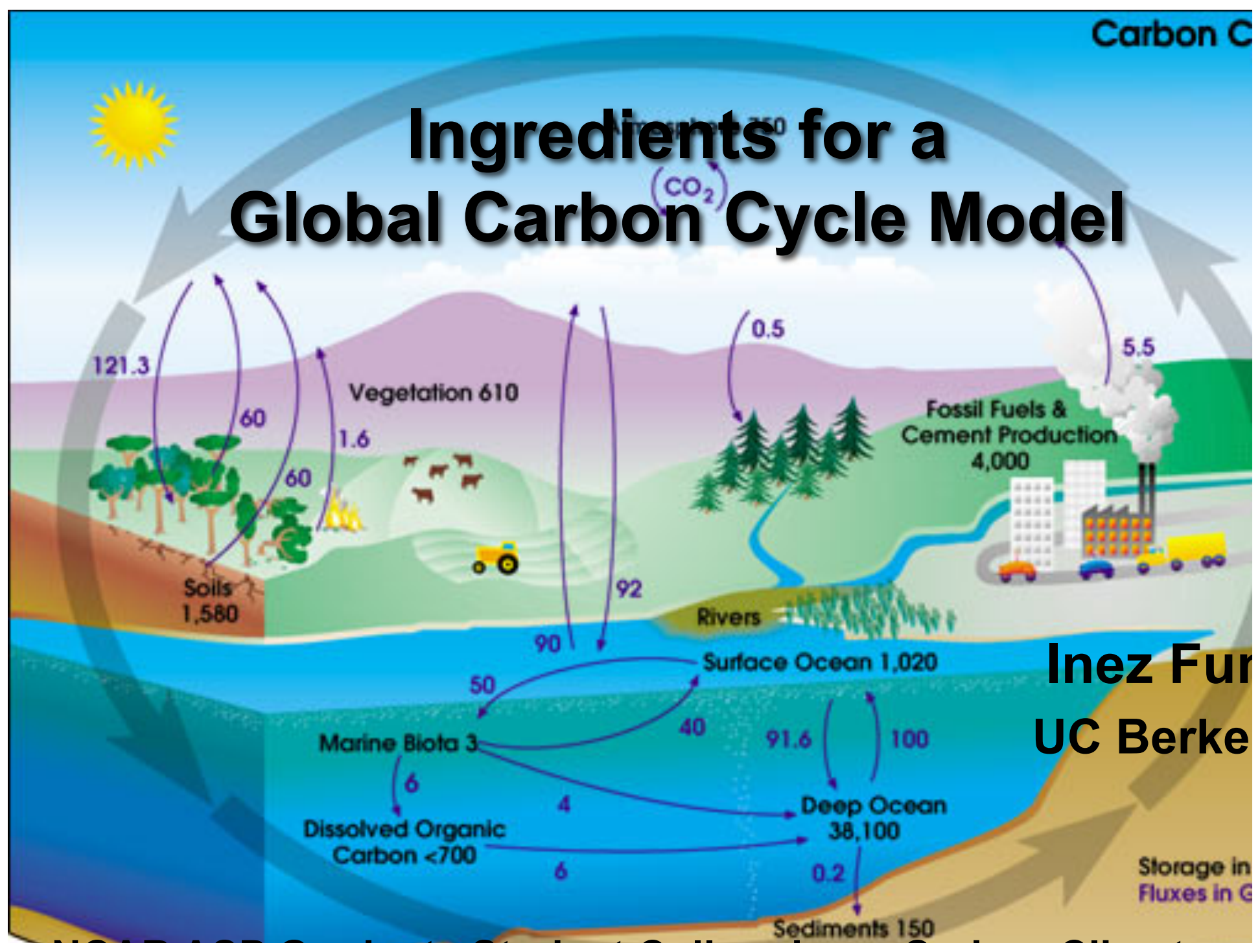


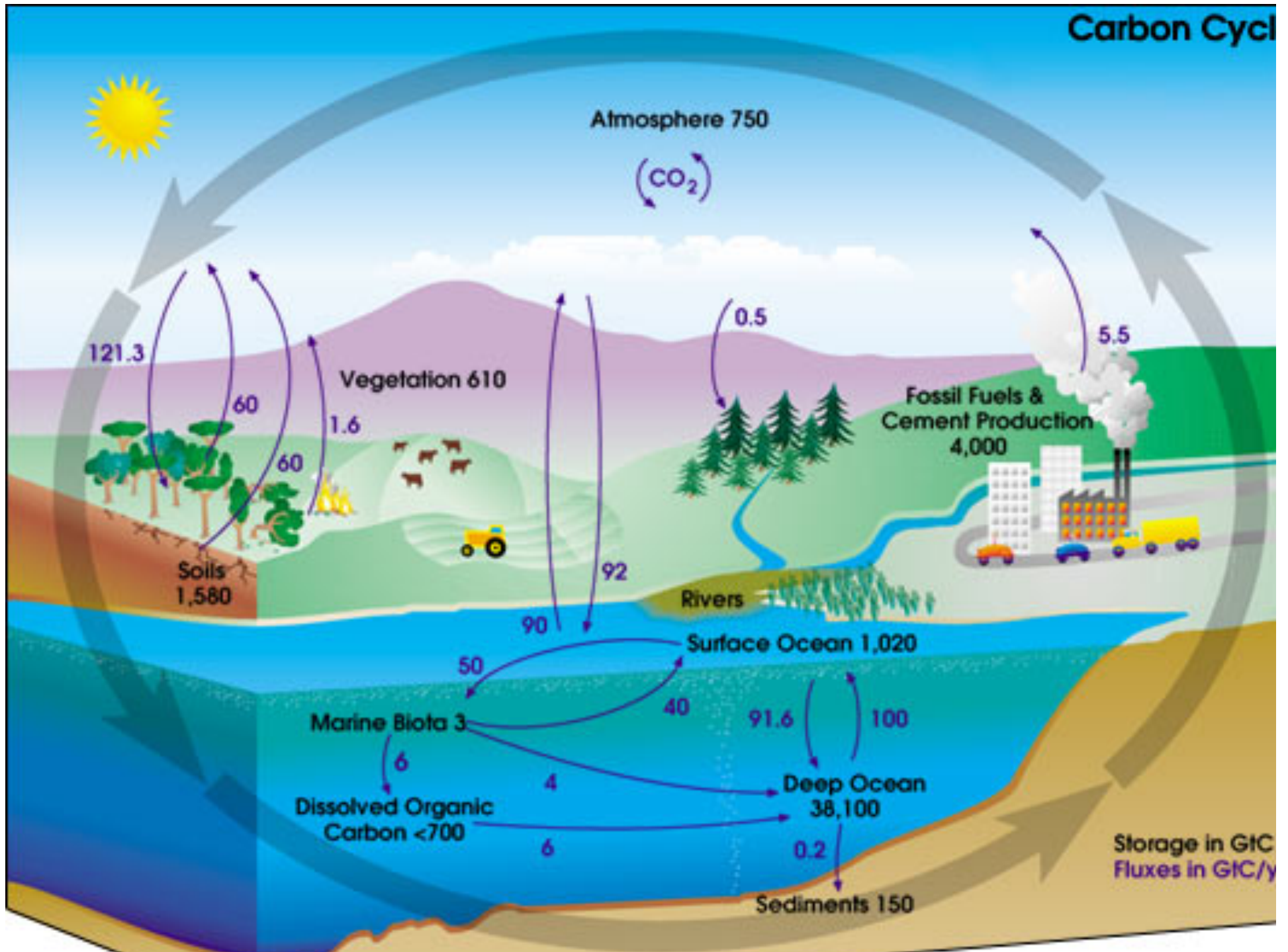
Ingredients for a Global Carbon Cycle Model



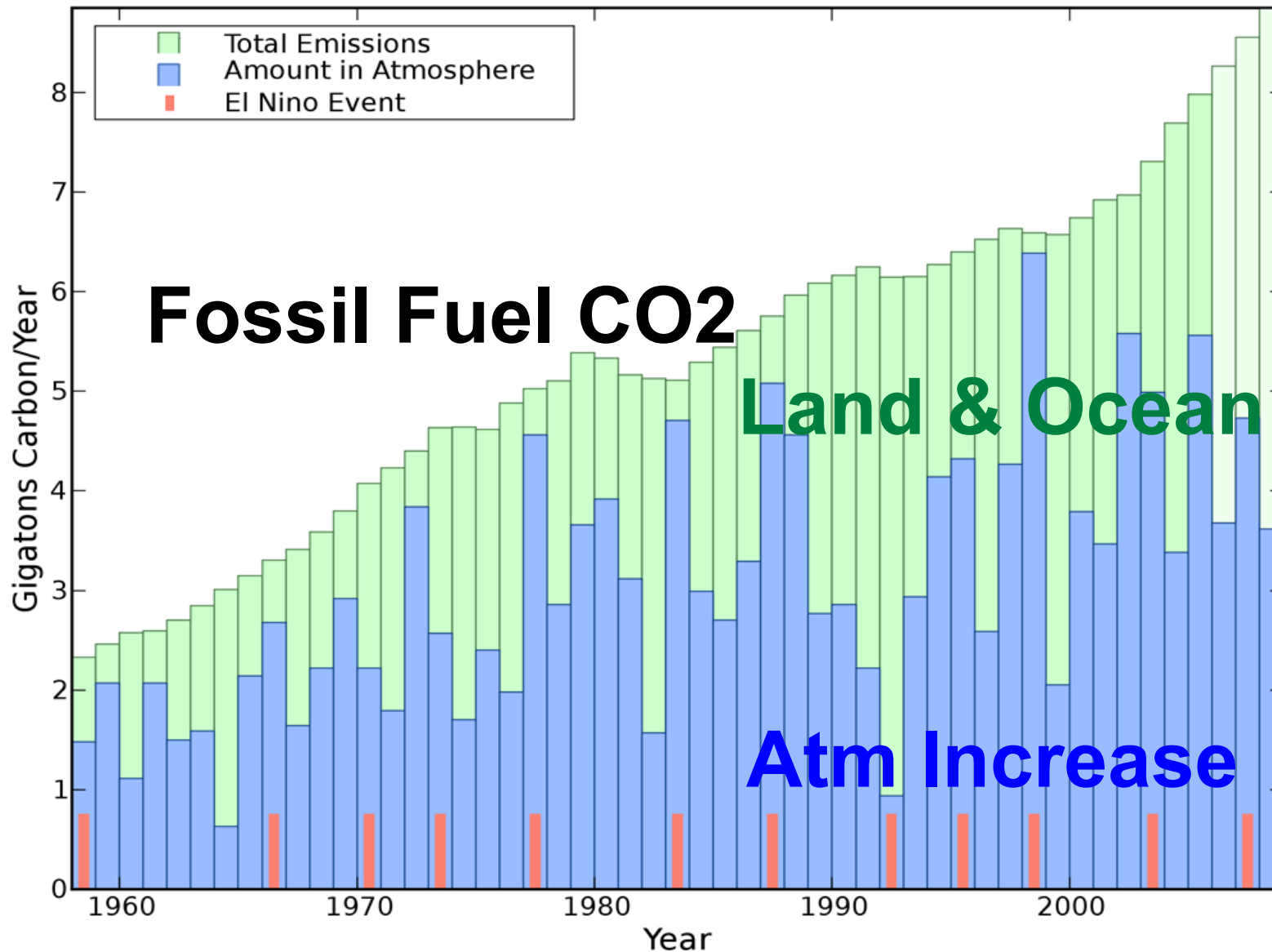
Inez Fur
UC Berke

Storage in
Fluxes in G

Carbon Cycle



Challenge: Co-variation of Climate and Carbon Sinks



Focus of Coupled Carbon Climate Model

- Changes in CO₂ and $\frac{\partial CO_2}{\partial t}$ that are radiatively important
- Time scale of investigation:
 - **Eqm**: e.g. Last Glacial Max; 2xCO₂
 - **Transient**: modern (now +/- several centuries). Leave out geology (and interactions with geology) if using complex Earth System Model.

Units: 1 Pg = 1 Gt = 10^{15} gram

$$C(\text{kgC} / \text{m}^3) = \rho(\text{kgAir} / \text{m}^3) \times X(\text{moleC} / \text{moleAir}) \times (\text{MWt}_C / \text{MWt}_{\text{air}})$$

$$\text{MWt}_C = 12 \text{ gm} / \text{mole}; \text{MWt}_{\text{air}} = 29 \text{ gm} / \text{mole}$$

$$\text{Area} = \int dx dy dz = 5 \times 10^{14} (\text{m}^2)$$

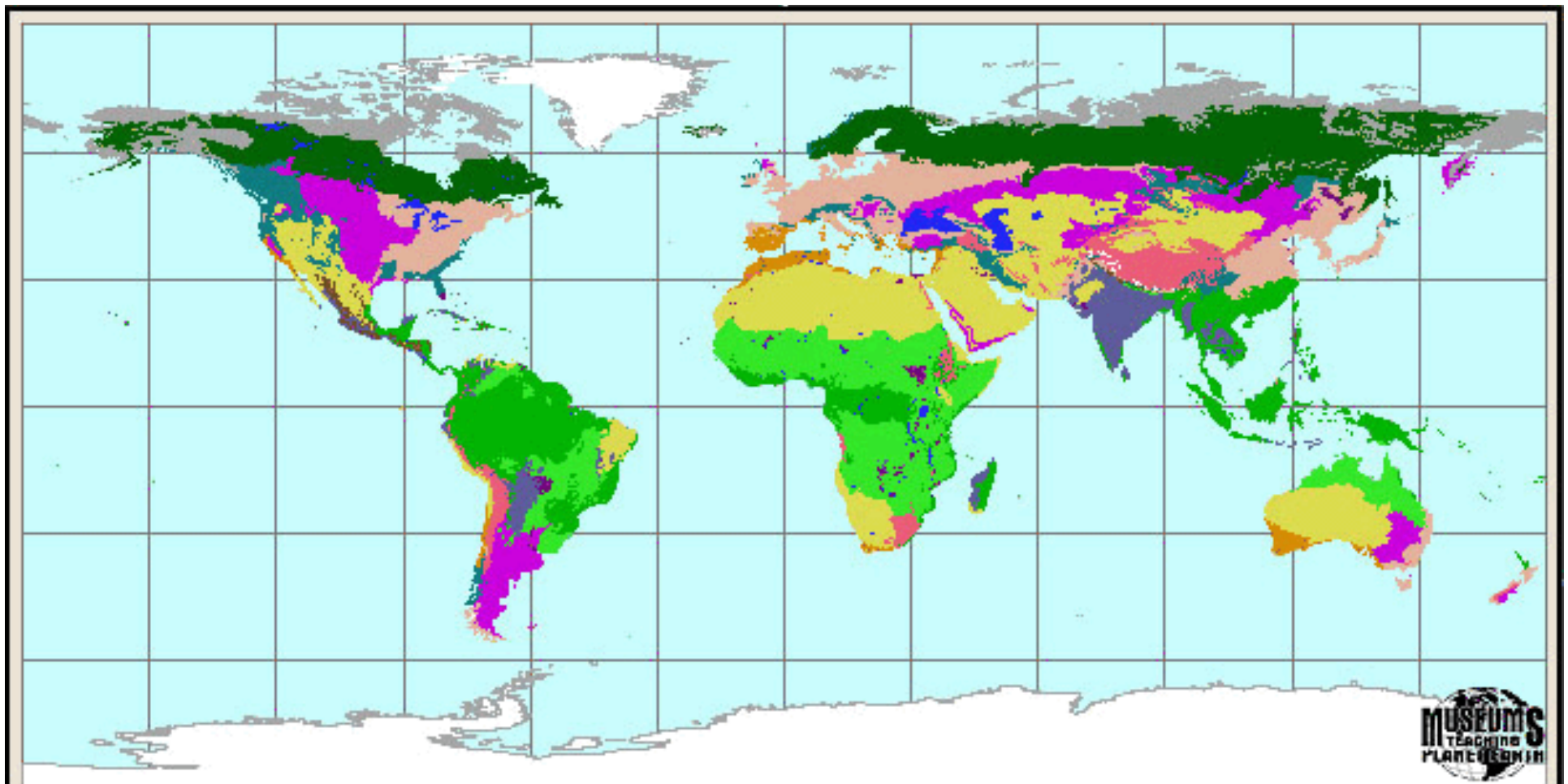
$$\text{MassAtm} = \int \rho dx dy dz = \frac{100 P_{mb}}{g} (\text{kgAir} / \text{m}^2) \times \text{Area} \sim 5 \times 10^{18} \text{ kgAir}$$

$$\text{MassC}(300 \text{ ppmv}) = \text{MassAtm} \times (300 \times 10^{-6}) \times (12/29)$$


$$\sim 600 \times 10^{12} \text{ kg} = 600 \text{ PgC} = 600 \text{ GtC}$$

$$1 \text{ PgC} \rightarrow 0.5 \text{ ppmv}(\text{mixed_entireAtm})$$

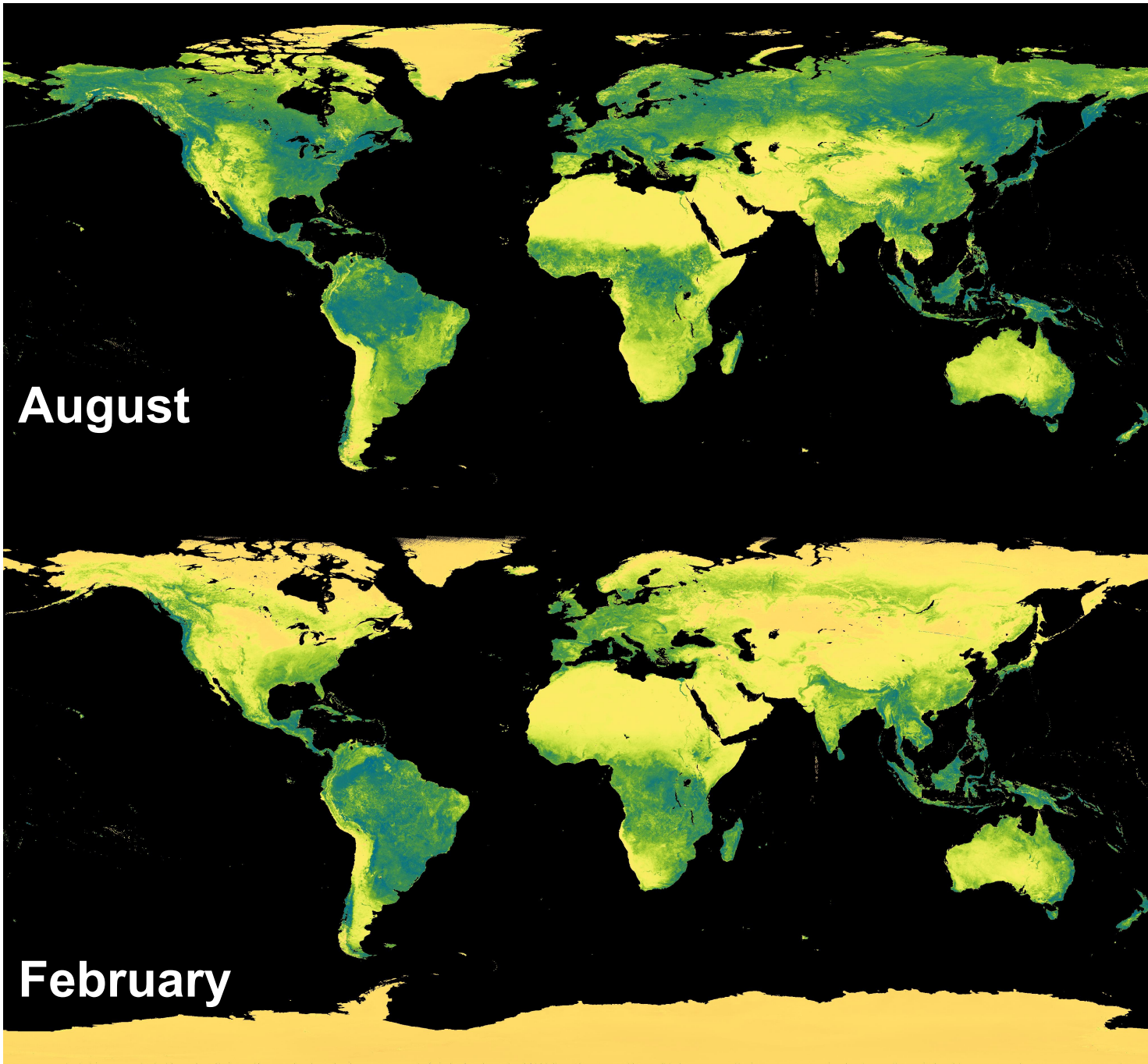
LAND BIOSPHERE



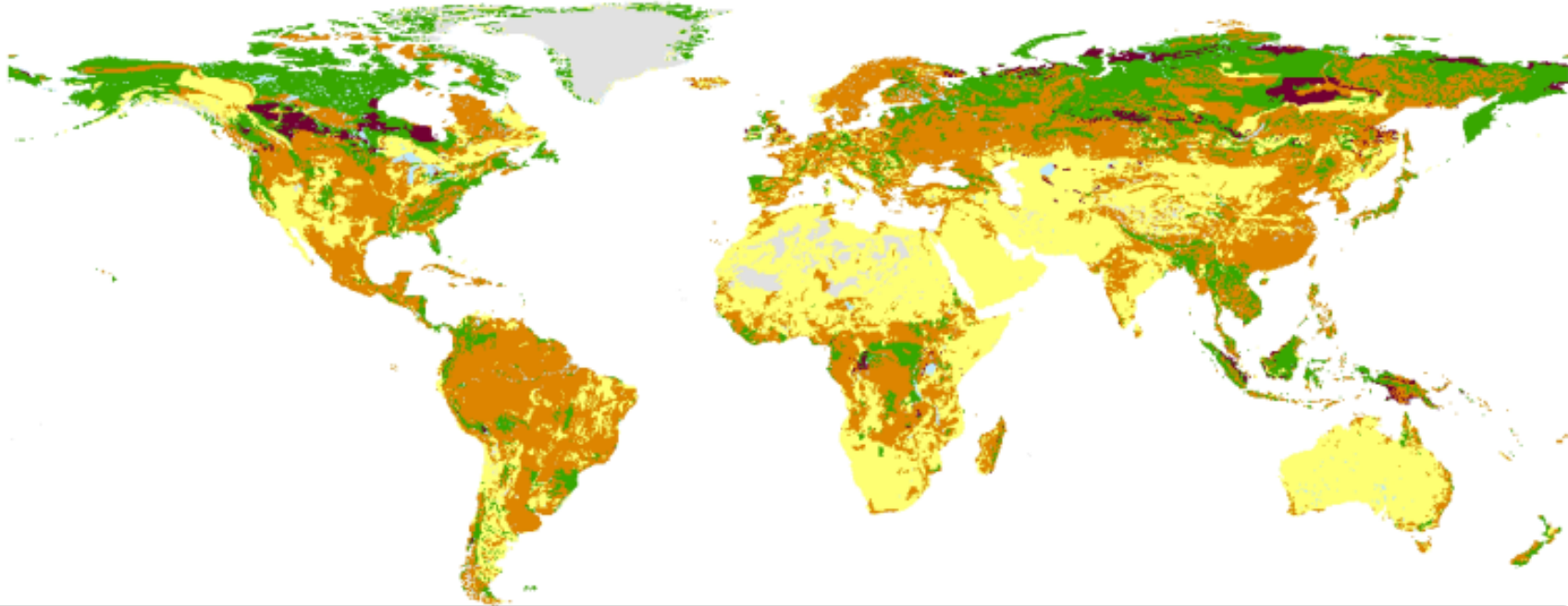
Earth's Biomes

- | | |
|---|---|
|  Boreal forests/taigas |  Temperate grasslands, savannas, and shrublands |
|  Deserts and xeric shrublands |  Tropical and subtropical coniferous forests |
|  Flooded grasslands |  Tropical and subtropical dry broadleaf forests |
|  Mangroves |  Tropical and subtropical grasslands, savannas, and shrublands |
|  Mediterranean scrub |  Tropical and subtropical moist broadleaf forests |
|  Montane grasslands |  Tundra |
|  Snow, ice, glaciers, and rock |  Inland Water |
|  Temperate broadleaf and mixed forests | |
|  Temperate coniferous forests | |

**Satellite
Greenness
index: NDVI**



Organic carbon pool (kg/m²/m) - Topsoil



Legend

VALUE

< 1.8 kg/m²

1.8 - 3.6 kg/m²

> 3.6 - 7.5 kg/m²

> 7.5 - 15.0 kg/m²

Water

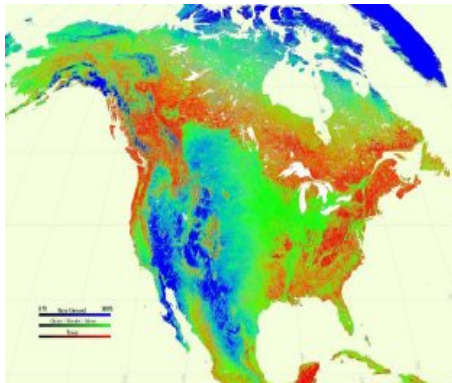
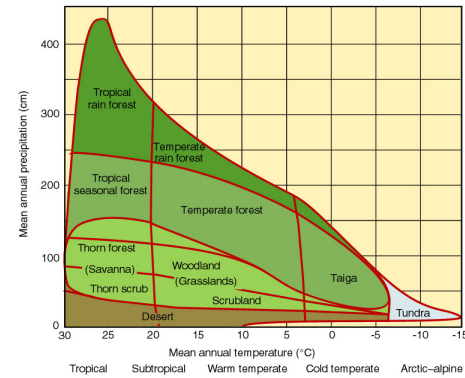
Glaciers, Rock, Shifting sand, Missing data

Source: FAO-UNESCO Soil Map of the World Geographic Projection: AGL-2007

High soil carbon found when there is abundant organic matter input, and slow decomposition (cold, not well aerated).

(1) Who: Name Calling

1. Taxa/Species
2. **Physionomic/structural**: Biomes e.g. desert, rainforest - albedo, roughness
3. **Bioclimatic + CO2 + ...**
4. **Functional**: based on satellite photosynthesis index:



$$\{\%tree / shrub\} \times \left\{ \begin{array}{l} deciduous \\ evergreen \end{array} \right\} \times \left\{ \begin{array}{l} broadleaved \\ needleleaved \end{array} \right\}$$

$$\{\%herbaceous / crops\} \times \left\{ \begin{array}{l} C3 \\ C4 \end{array} \right\}$$

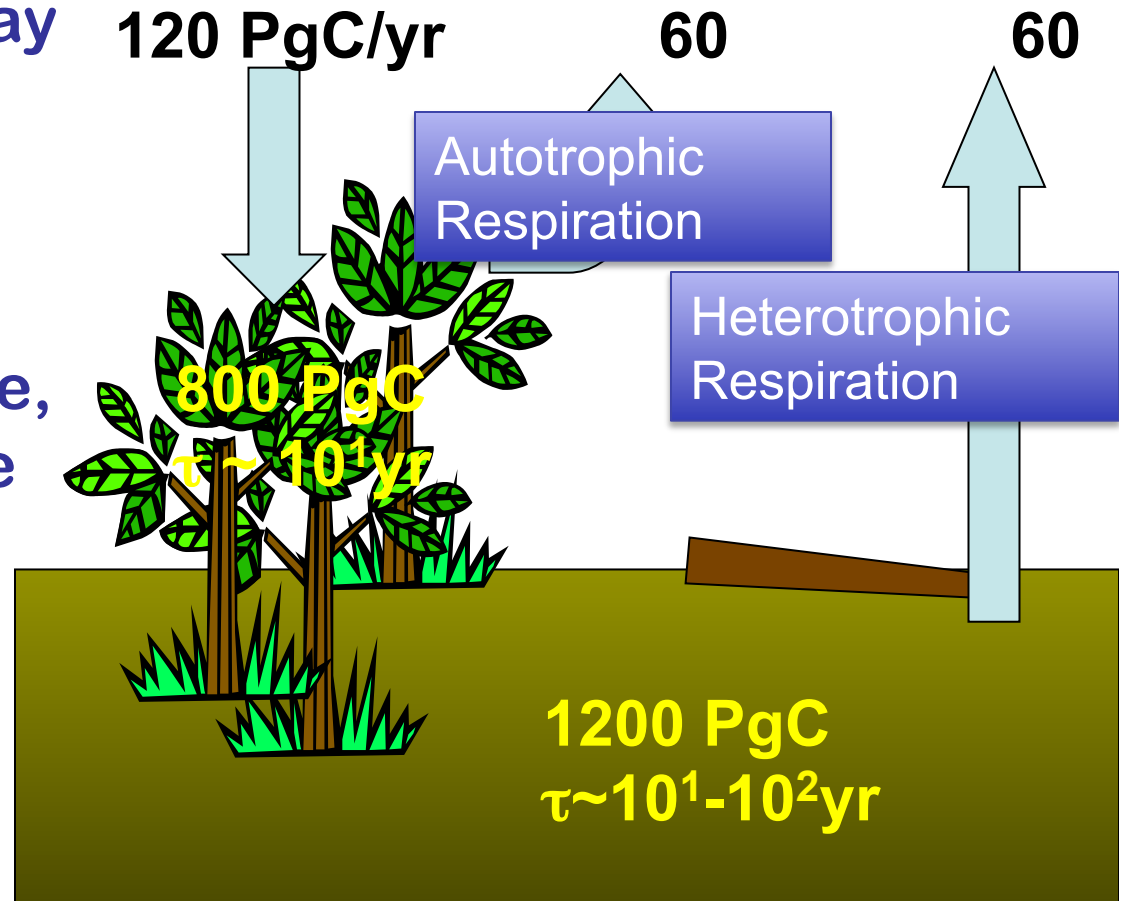
$$\{\%bare\}$$

Static land cover: typically 4 --> lookup table of structural properties and BGC characteristics. Prognostic land cover: 3+

(2) What? [lifecycle traced by C cycle]

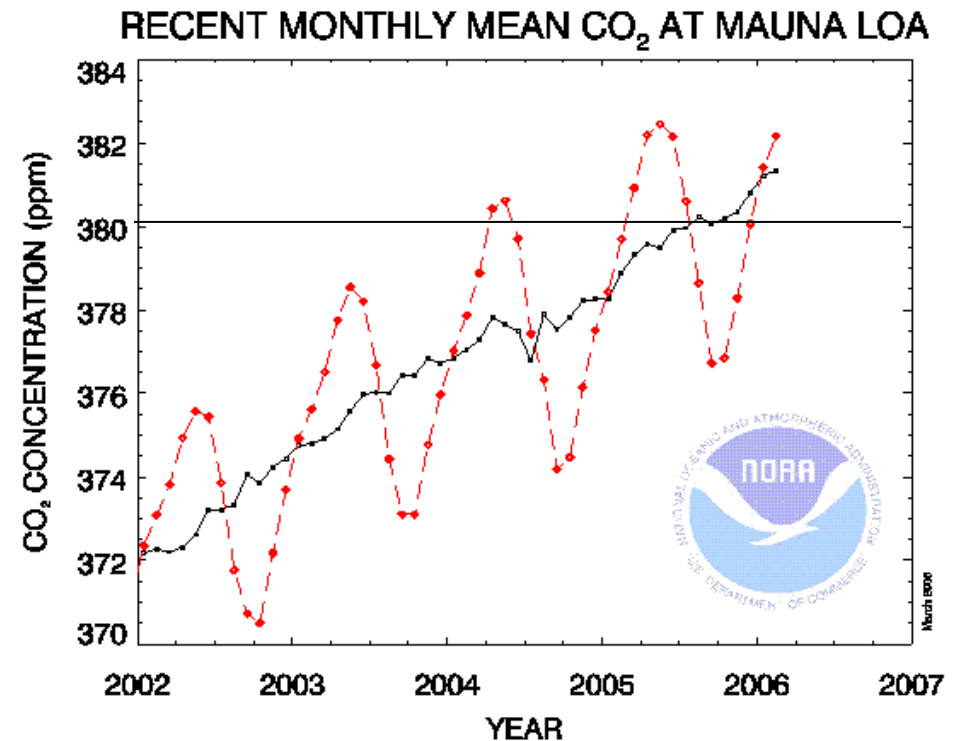
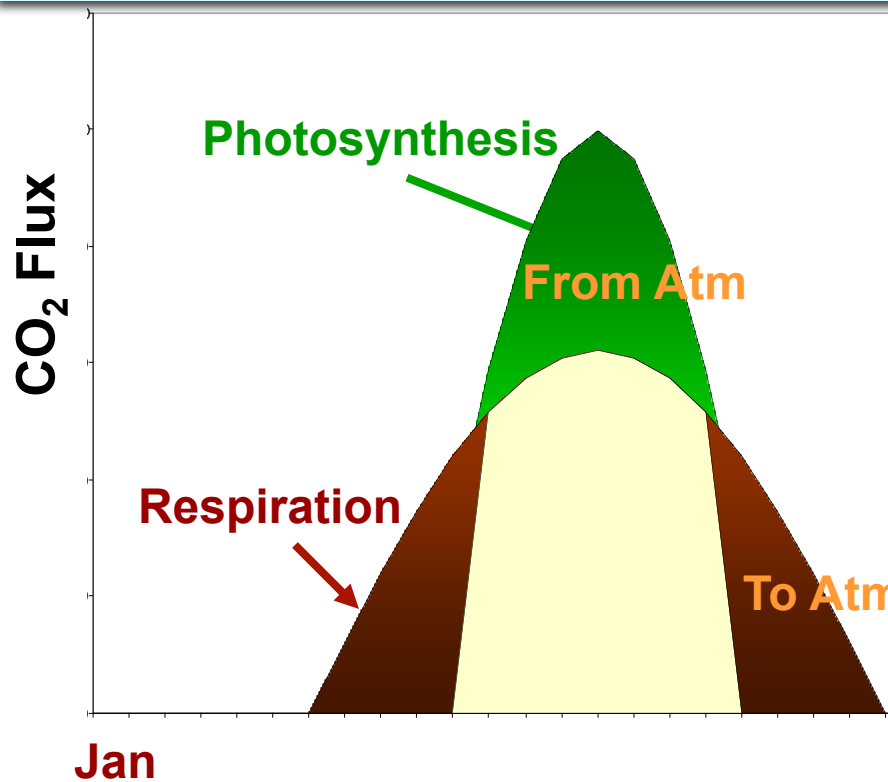
Gross Primary Productivity

- Growth, mortality, decay
- Population: {ages}
- Photosynthesis (climate, CO_2 , soil H_2O , resource limitation)
- Decay (T, soil H_2O ,...)



$$\text{Net Primary Production (NPP)} = \text{GPP} - R_{\text{auto}}$$

Two major fluxes - seasonal cycle



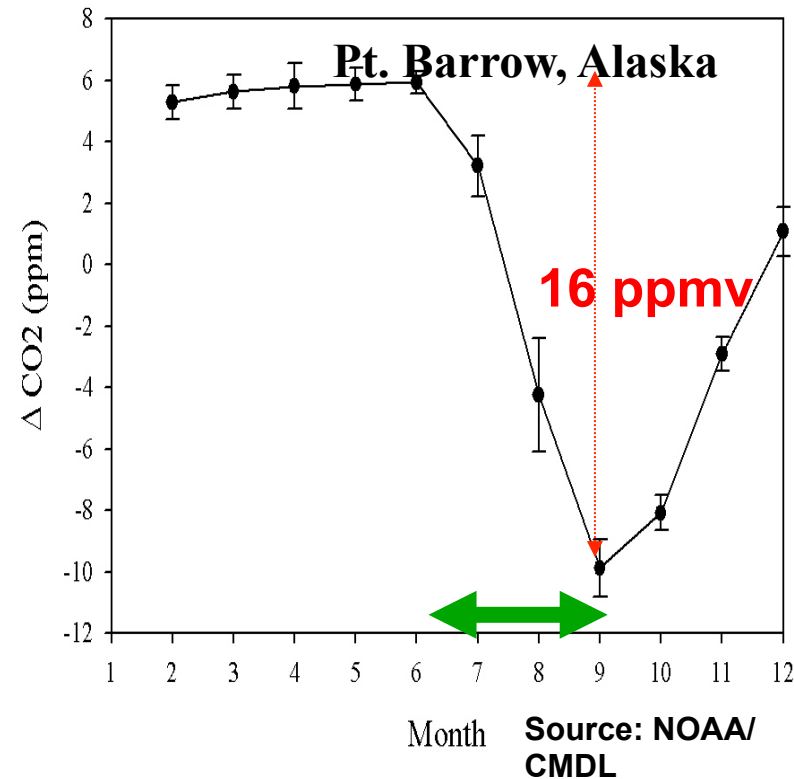
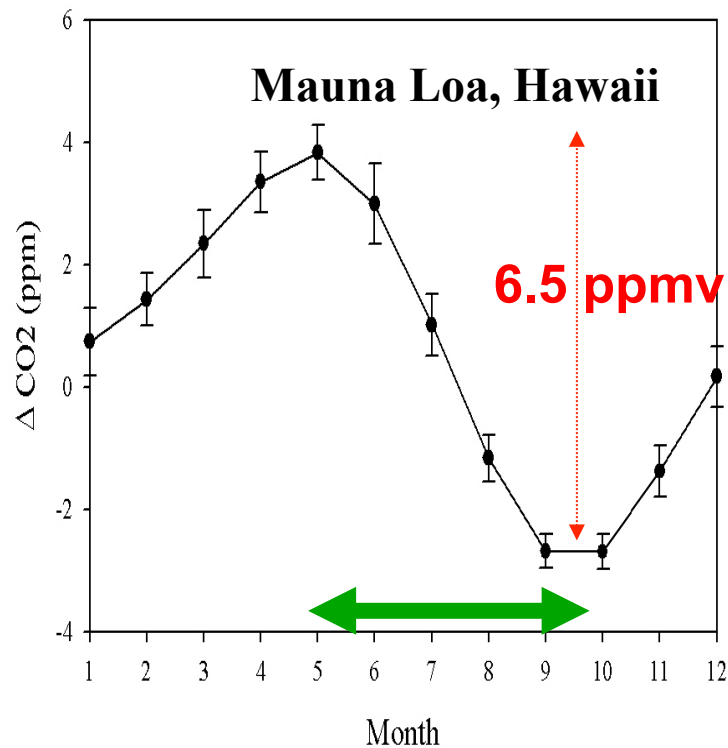
- **Seasonal asynchrony** between photosynthesis and decomposition

→ net fluxes of CO₂ to and from atm
→ seasonal cycle of CO₂ in atm

- **Annual imbalance** → carbon source/sink

Fung et al JGR 1983, 1987:
Simple prescriptions of seasonality. 1987 based on satellite obs + temperature

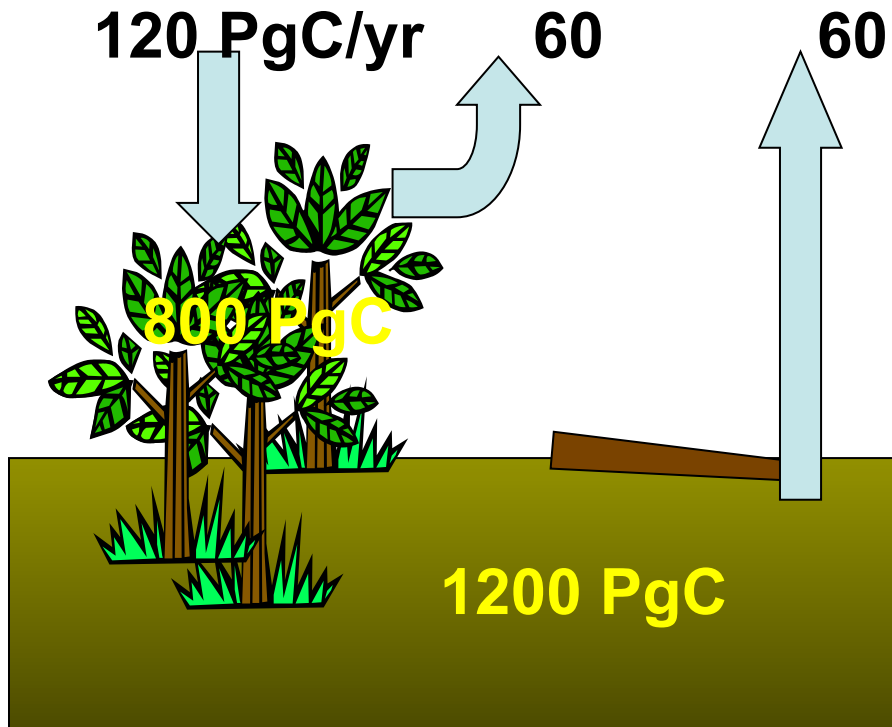
Atmospheric CO₂ Signature of Ecosystem C Exchange: Seasonal Cycle



- Amplitude of atmospheric CO₂ seasonal cycle increases poleward: telecoupling of growing season and greater asynchronicity bet' fluxes
- Growing season net flux ~15-20% of annual NPP

(3.1) How?

First simple toy model: carbon only

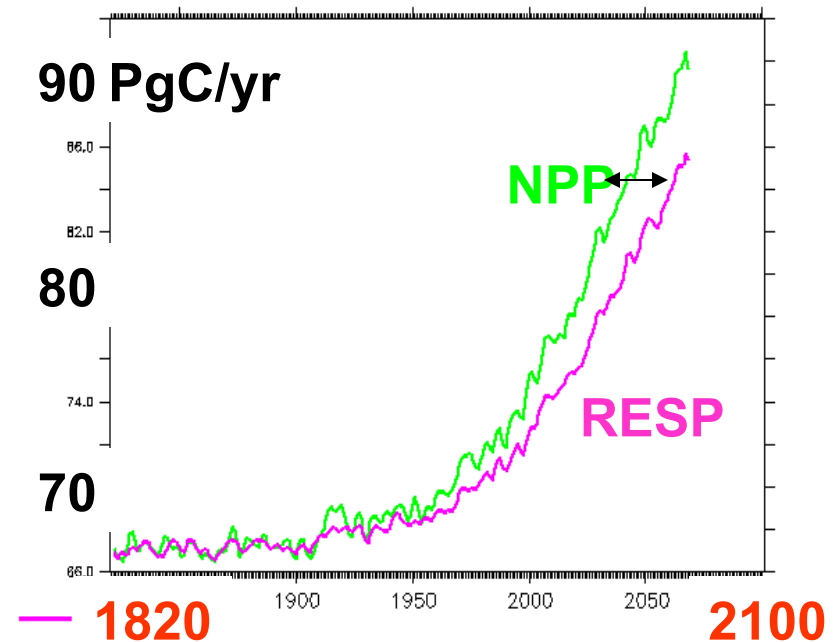


$$\frac{\partial M_{veg}}{\partial t} = NPP - \frac{M_{veg}}{\tau_{veg}}$$
$$\frac{\partial M_{soil}}{\partial t} = \frac{M_{veg}}{\tau_{veg}} - (1 - \gamma) \frac{M_{soil}}{\tau_{soil}} - \underbrace{\gamma \frac{M_{soil}}{\tau_{soil}}}_{Het\ Resp}$$

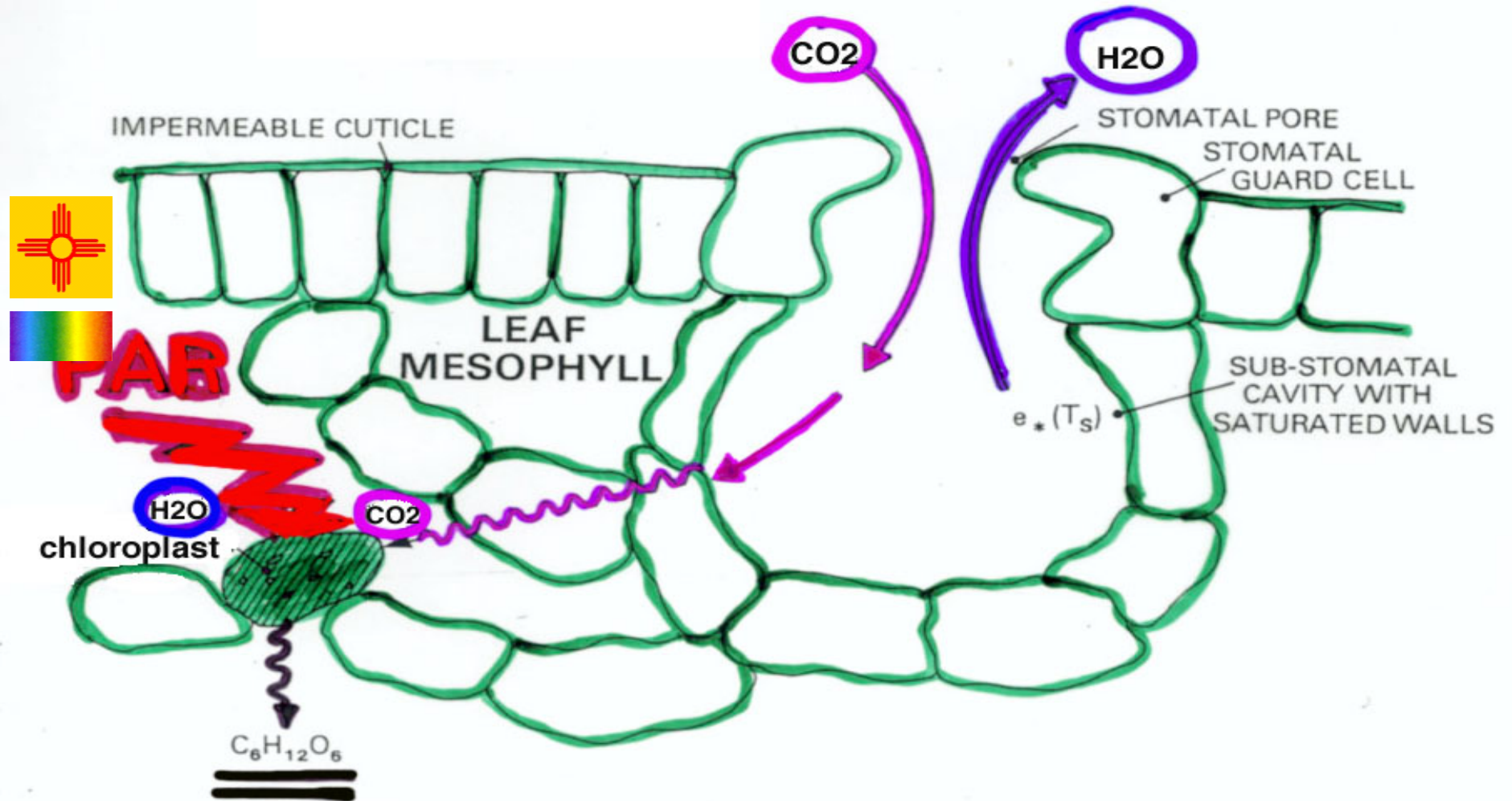
Turnover times (climate)

$$\tau_{veg} \sim 15 \text{ yr}$$

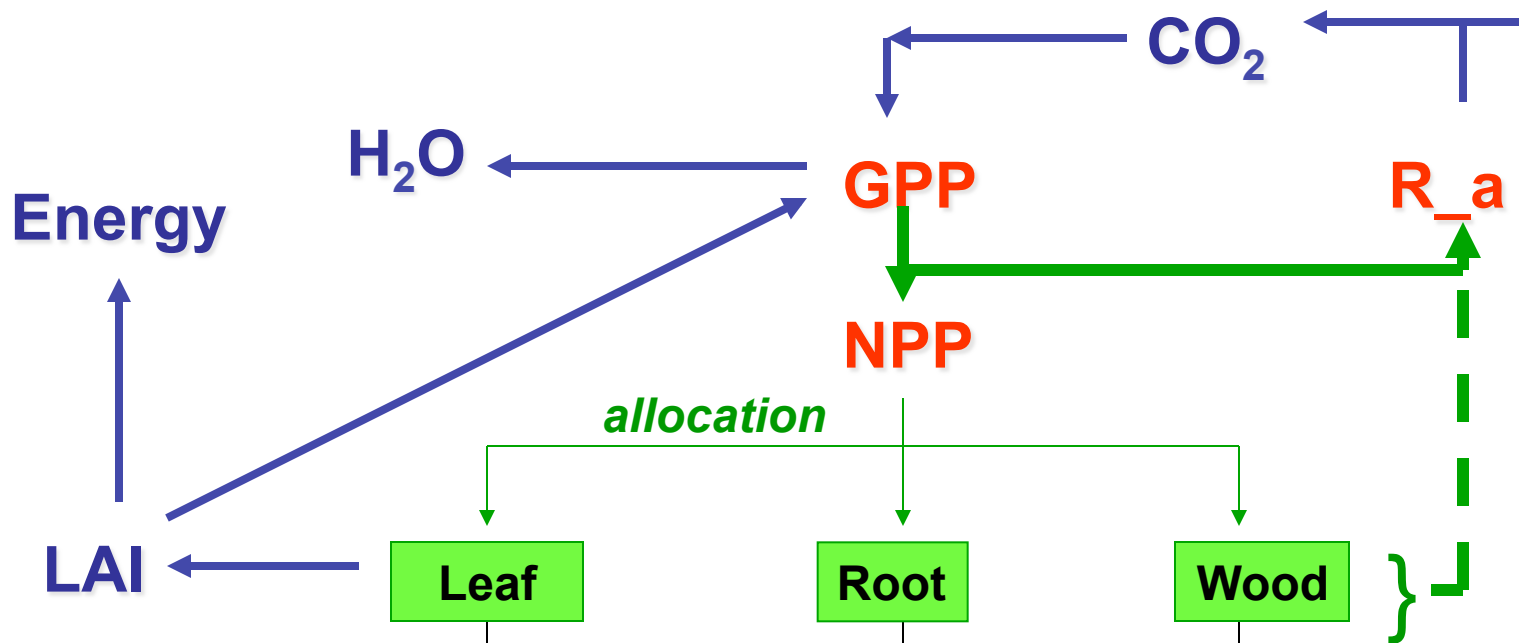
$$\tau_{soil} \sim 25 \text{ yr}$$



(3.2.1) Leaf Photosynthesis

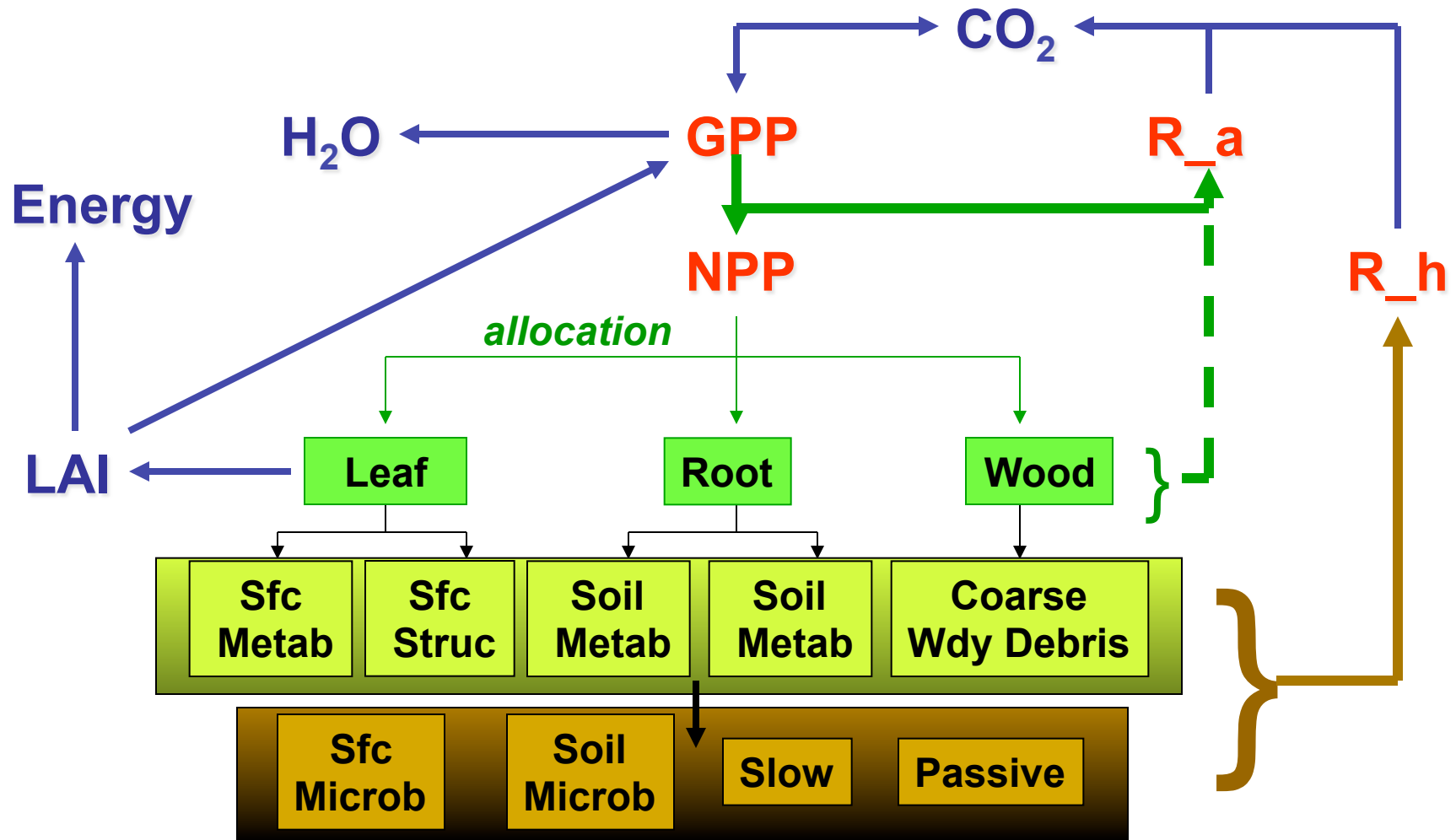


(3.2.2) Photosynthesis --> Growth



Strategy for survival: allocate new C to
Roots when water and nutrient limited
Wood when light limited

(3.2.3) Photosynthesis, Growth, Mortality & Decay



(3.3) Prognostic Carbon Cycle (with transpiration and dynamic albedo)

Atm

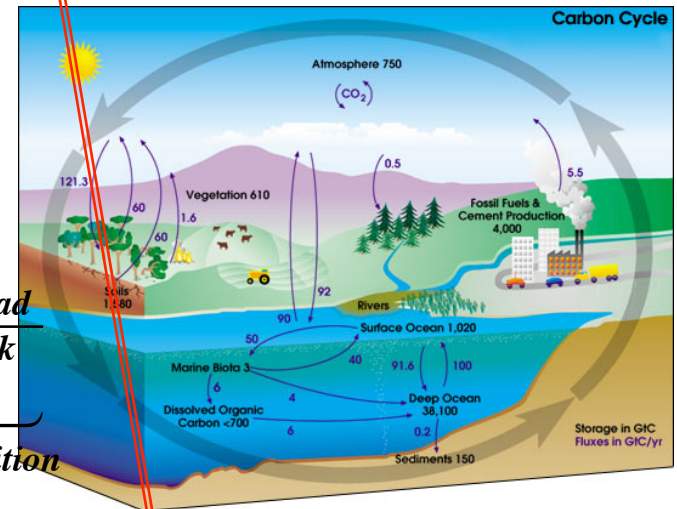
$$\frac{DC_a}{Dt} = (FF + Def + \underbrace{F_{oa} \updownarrow}_{\text{air-sea flux}} + \underbrace{F_{ba} \updownarrow}_{\text{atm-land flux}}) + \mathfrak{S}(C_a)$$

Land-live

$$\frac{\partial C_{b_live}^k}{\partial t} = -\alpha^k \underbrace{F_{ab} \downarrow}_{\text{photosynthesis}} - \underbrace{\frac{C_{b_live}^k}{\tau_{live}}}_k$$

Land-dead

$$\frac{\partial C_{b_dead}^k}{\partial t} = \underbrace{\frac{C_{b_live}^k}{\tau_{live}}}_k + \sum_j F_{jk} - \underbrace{\frac{C_{b_dead}^k}{\tau_{dead}}}_k$$

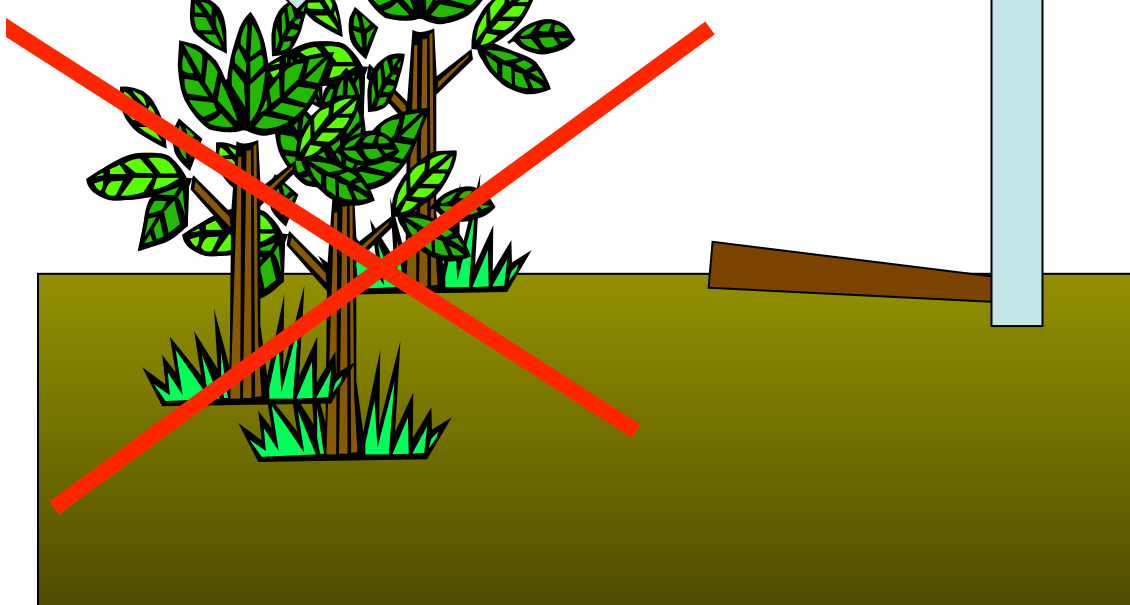
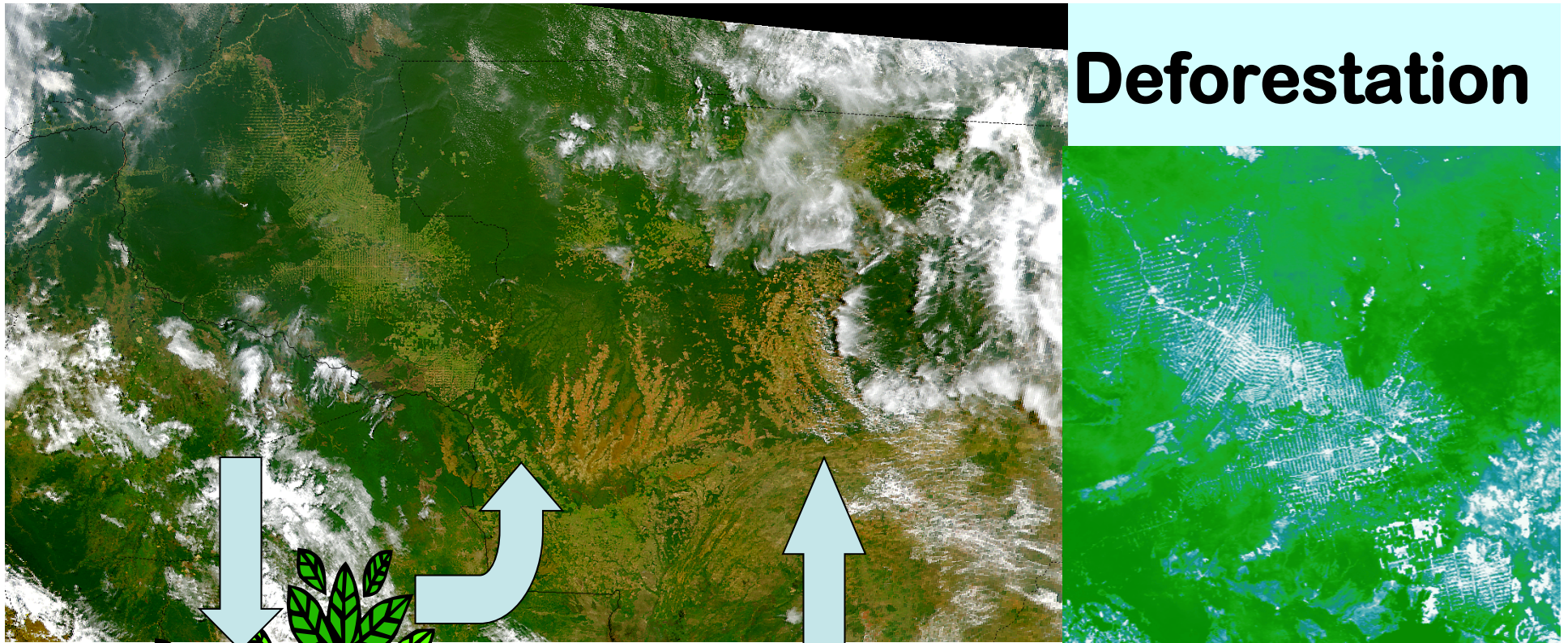


Changes climate

Responds to climate change

DEFORESTATION

Deforestation

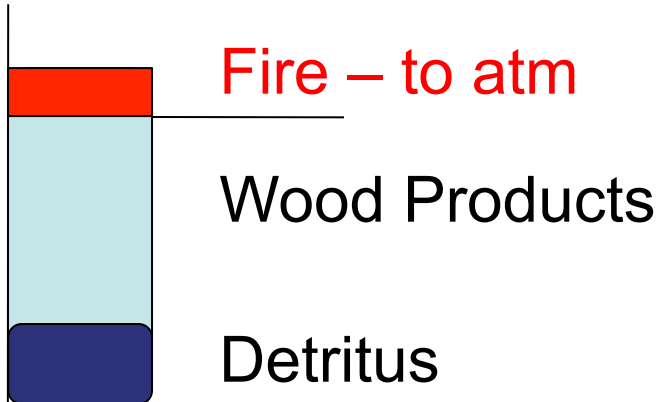


Tough to estimate

- deforested area
 - Carbon inventory before deforestation
 - Fate of removed carbon
 - Fate of litter and soil carbon
- Tough to discriminate atm CO₂ signature**

Fate of Carbon

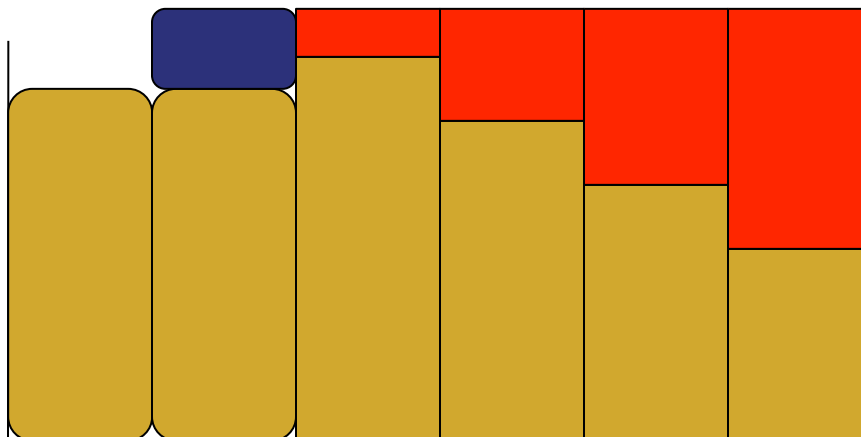
Above ground carbon



Cropping cycle: accumulate above ground carbon during growth. Carbon balance depends on the treatment of the detritus, time between crop and fallow, tilling practice,...

time

Below ground carbon

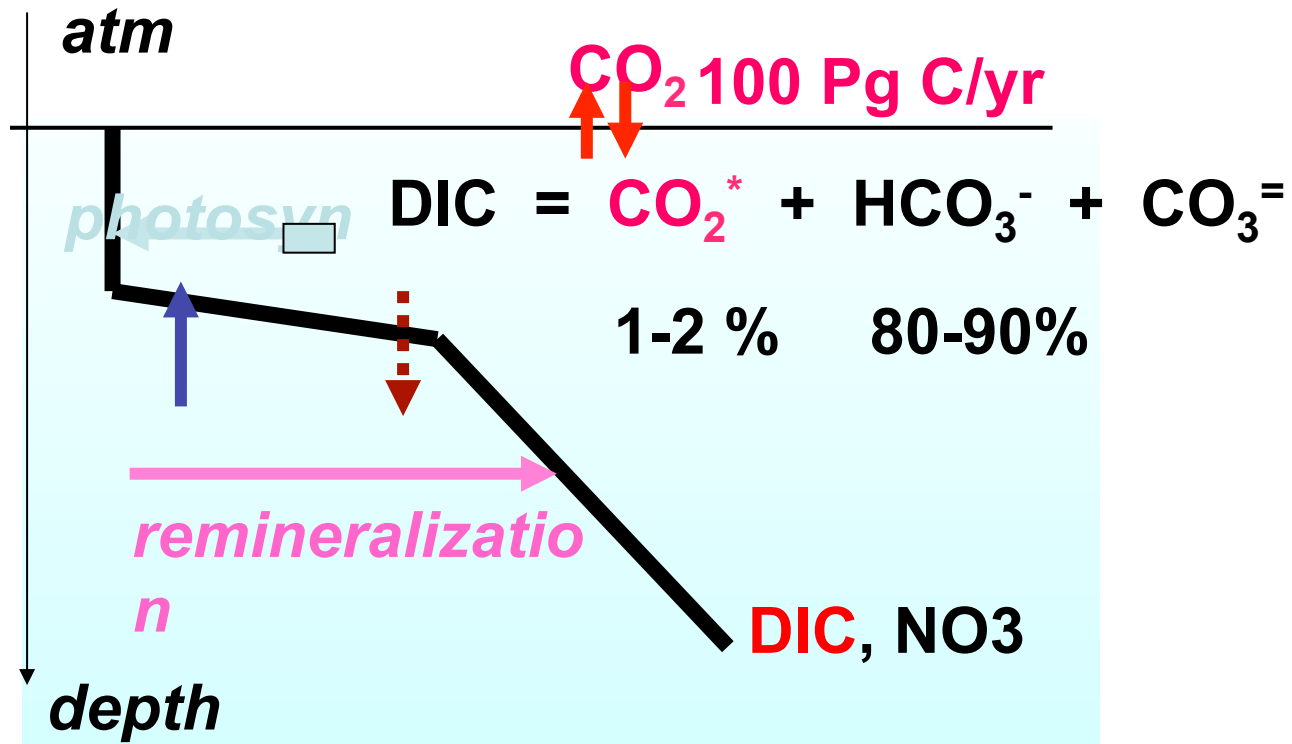


Decomposition – to atm

time

OCEAN CARBON

Ocean C from the Atm' s Perspective:



$$F_{oa} - F_{ao} = \underbrace{k}_{\text{GasExchRate}(m/s)} \times \left(\underbrace{\text{CO}_2^*_{\text{sfc_ocn}}}_{\text{moleC}/m^3} - \underbrace{\beta}_{\text{solubility}(T)} \times p\text{CO}_2_{\text{atm_sfc}} \right)$$

(1) Simplified Carbonate Chemistry

Chemical Equilibrium



$$K(T,S) = \frac{[\text{HCO}_3^-][\text{HCO}_3^-]}{[\text{CO}_2][\text{CO}_3^{=}]}$$

Mass and Charge Balance

$$\Sigma \text{CO}_2 = \text{TC} = \text{DIC} = \text{CO}_2 + \text{HCO}_3^- + \text{CO}_3^{=}$$

CO₂ increases with increasing DIC

$$\text{ALK} = \text{HCO}_3^- + 2[\text{CO}_3^{=}]$$

CO₂ decreases with increasing ALK

Henry's Law

$$p\text{CO}_2 = k_H * \text{CO}_2$$

pCO₂ : partial pressure (CO₂ gas), in atm

Atm View: Summary of Carbonate Chemistry

$$\frac{\partial}{\partial t}(h \cdot DIC) = k \cdot solub \cdot pCO2_a - k \boxed{CO2_{ml}} + Prod_bio - Loss_bio$$

$$\frac{1}{CO2^*} d(CO2^*) = d(\ln(CO2^*))$$

$$= \underbrace{\frac{d \ln CO2^*}{d \ln DIC}}_{\sim 10} d \ln DIC \quad \text{Revelle factor}$$

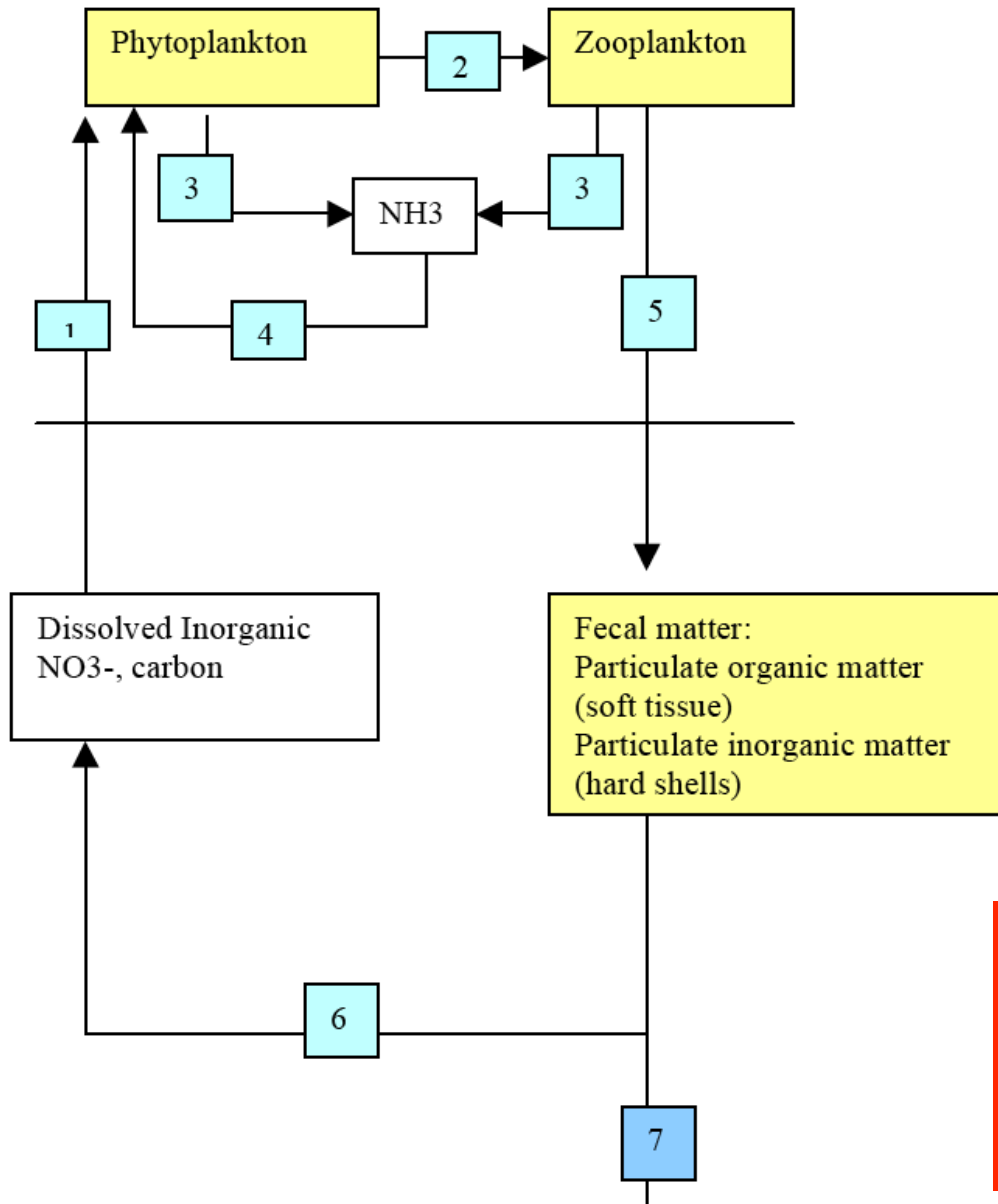
$$+ \underbrace{\frac{d \ln CO2^*}{d \ln TALK}}_{\sim -9} d \ln TALK$$

$$+ \underbrace{\frac{d \ln CO2^*}{dT}}_{\sim 4\% / K} dT \quad \text{Solubility Pump}$$

$$+ \frac{d \ln CO2^*}{dS} dS$$

(2.1) Marine Biota – Biological Carbon Pump

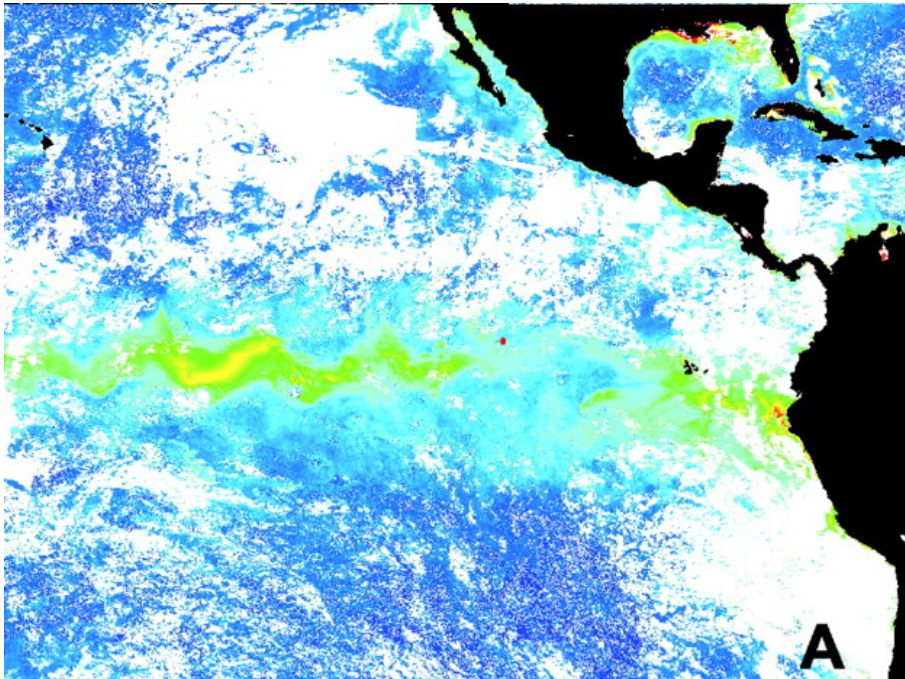
Mixed layer



1. Upwelling (new production)
2. grazing of phytoplankton by zooplankton
3. mortality and remineralization - bacteria
4. recycling: production
5. mortality of zooplankton, sinking, export from euphotic zone
6. remineralization
7. sinking to greater depths – carbonate dissolution or burial in sediments

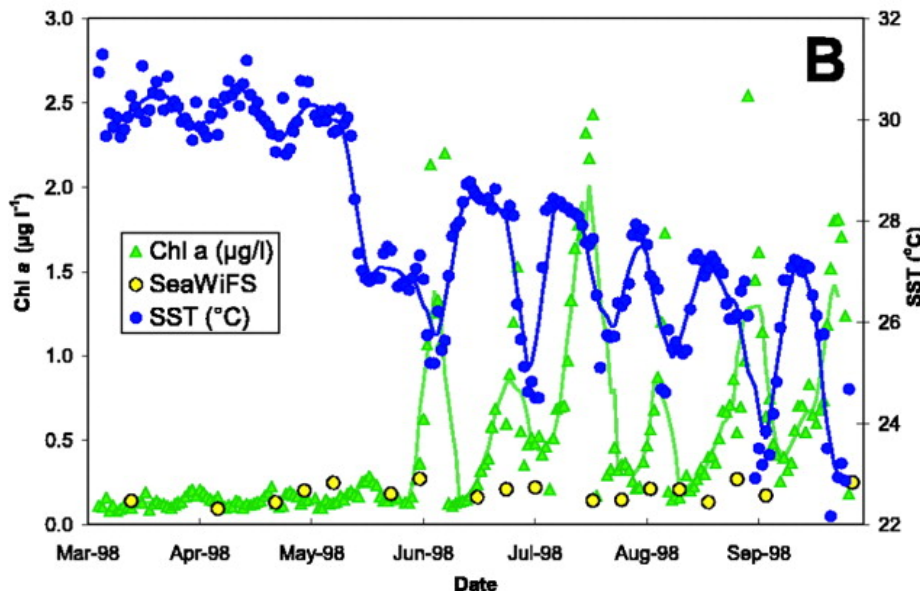
Dissolved Inorganic C
Dissolved Organic C
Particulate Inorganic C
Particulate Organic C

Marine Productivity



Is possible when **upwelling** brings:

- Nutrients from below to euphotic zone
- Cold water

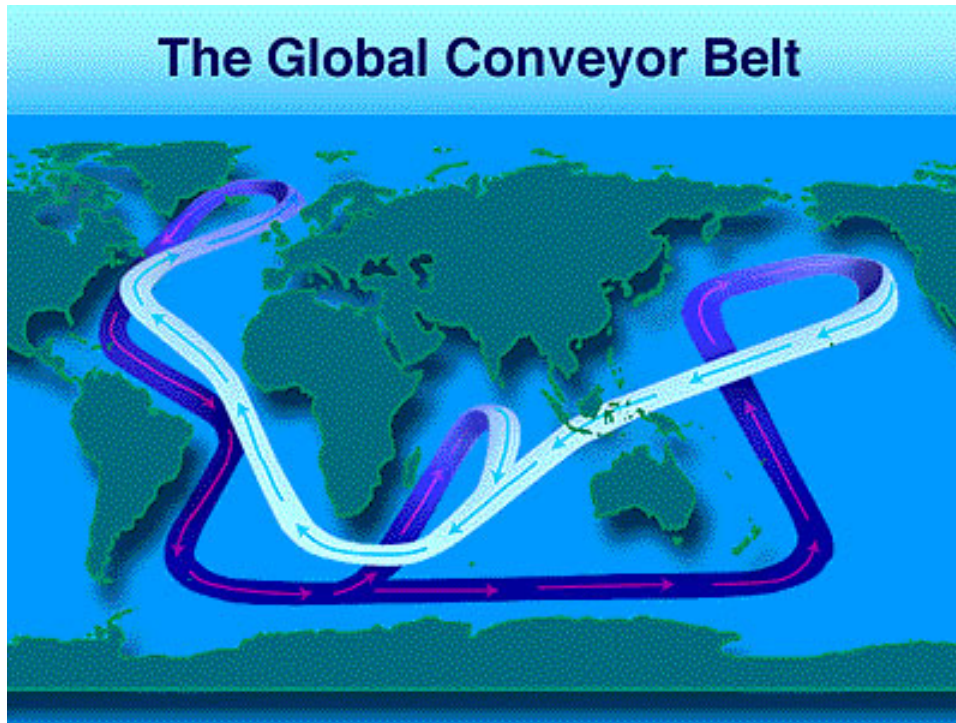


Small Flux, small inventory of organic C
But alters DIC(z)

Biological C Pump

Redfield ratio = C:N:P in organic matter ~103: 16: 1

		DIC	TALK	[CO ₂]
Formation of POC (surface ocean)	$\text{CO}_2 + \text{H}_2\text{O} \rightarrow \text{CH}_2\text{O} + \text{O}_2$; $\text{NO}_3^- + 2\text{H}_2\text{O} \rightarrow \text{NH}_3^+ + \text{OH}^- + 2\text{O}_2$	- 1 unit	+ (16/103)*1 (Redfield * charge)	↓
Formation of CaCO ₃ (surface)	$\text{Ca}^{++} + \text{CO}_3^{=} \rightarrow \text{CaCO}_3$	- 1 unit	- 2 units	↑
Remineralization of organic matter		+ 1 unit	- 16/103	↑
Dissolution of shells		+ 1 unit	+ 2	↓

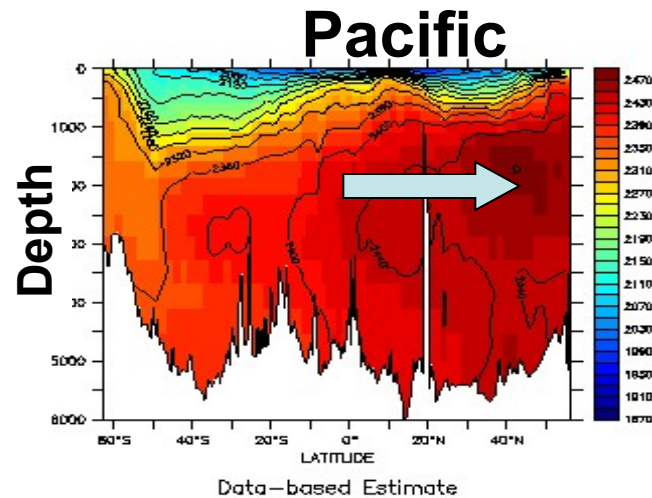
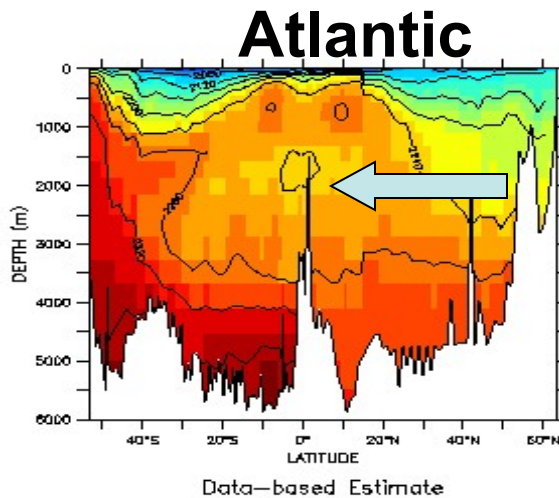


(2.3) OceanC : Mainly Dissolved Inorganic Carbon (DIC)

Conveyor Belt Transport of DIC:

- Southward in Atlantic
- Northward in Pacific

Ocn currents ~ cm/s
Time scale ~ 10^3 yr



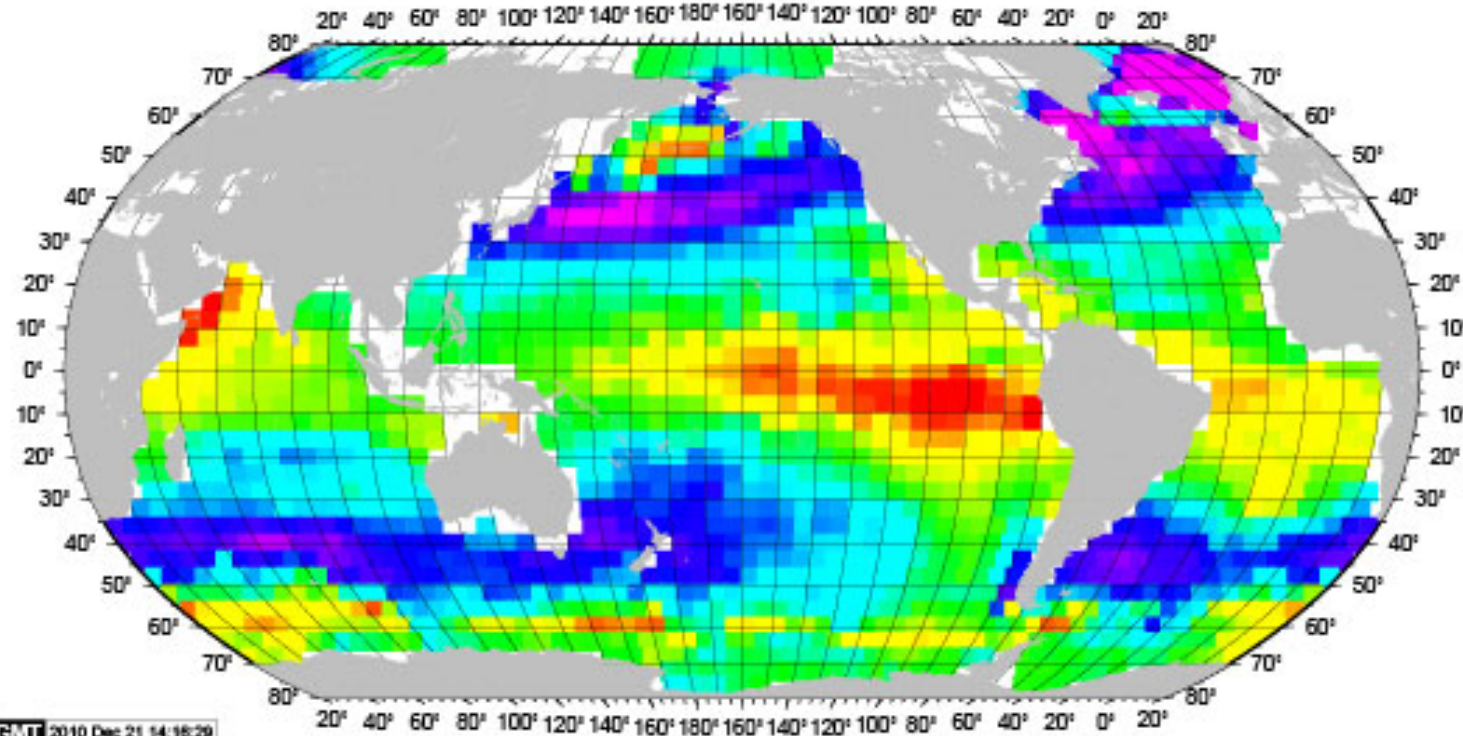
Latitude → N

Biology and DIC:

- Depletion near sfc
- Enrichment at Depth

First barrier to Ocean Uptake: Air-Sea CO₂ Flux

Mean Annual Air-Sea Flux for 2000 [Rev Dec 10] (NCEP II Wind, 3,040K, $\Gamma=0.26$)

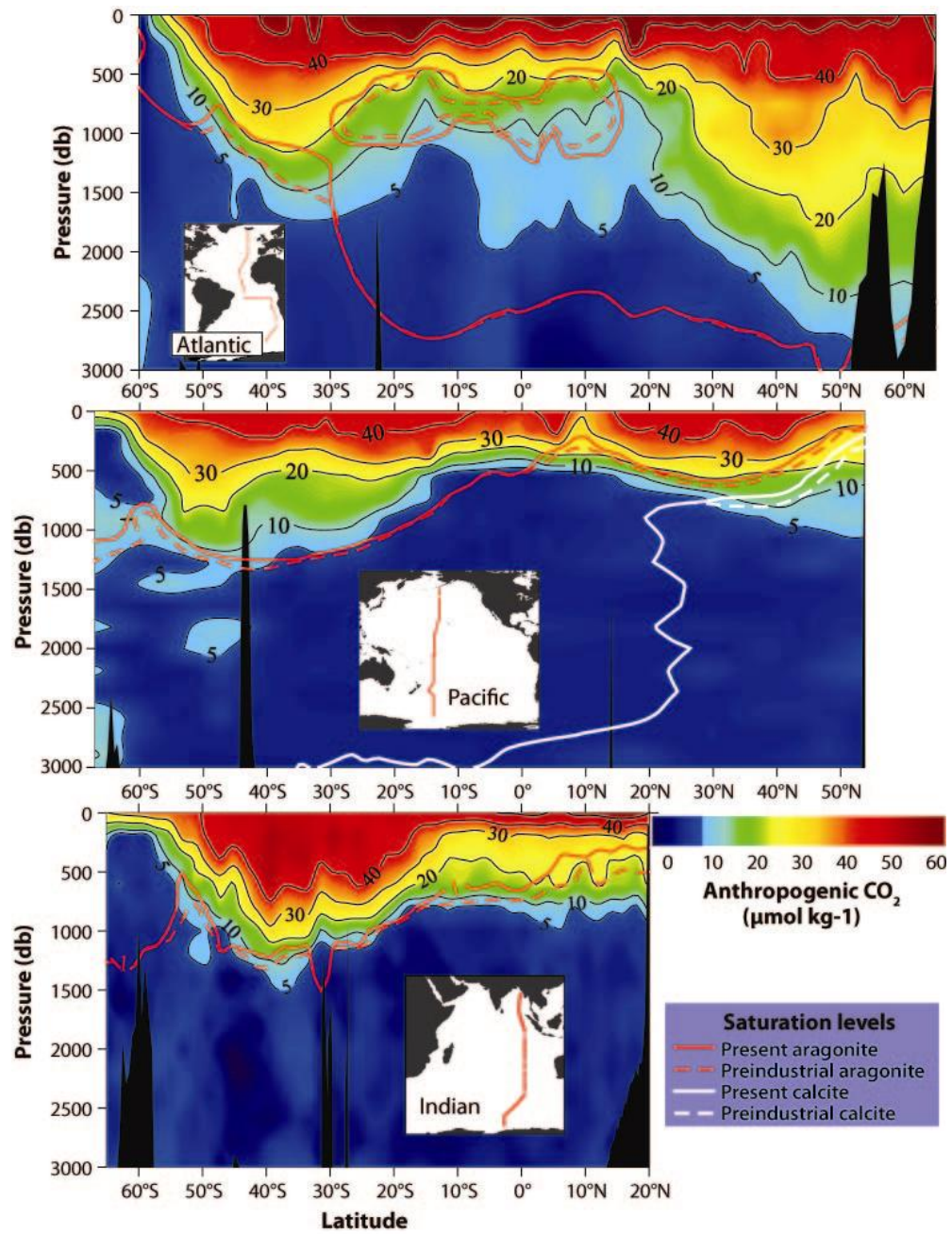


From Atm



To Atm

http://www.ldeo.columbia.edu/res/pi/CO2/carbondioxide/pages/air_sea_flux_2010.html



SUMMARY

Prognostic Carbon Cycle

Atm

$$\frac{\partial C_a}{\partial t} + \frac{\partial}{\partial x}(u_a C_a) + \dots = (FF + Def + \underbrace{F_{oa} \updownarrow}_{\text{air-sea_flux}} + \underbrace{F_{ba} \updownarrow}_{\text{atm-land_flux}}) \Big|_0 + \underbrace{\mathfrak{S}(C_a)}_{\text{turbulent_mixing}}$$

Ocean

$$\frac{\partial C_o}{\partial t} + \frac{\partial}{\partial x}(u_o C_o) + \dots = -F_{oa} \updownarrow \Big|_0 + \underbrace{P - L}_{\text{biology}} + \mathfrak{S}(C_o)$$

Land-live

$$\frac{\partial C_{b_live}^k}{\partial t} = -\alpha^k \underbrace{F_{ab} \downarrow}_{\text{photosynthesis}} \Big|_0 - \underbrace{\frac{C_{b_live}^k}{\tau_{live}^k}}_{\text{mortality}}; \quad \sum_k \alpha^k = 1$$

Land-dead

$$\frac{\partial C_{b_dead}^k}{\partial t} = \underbrace{\frac{C_{b_live}^k}{\tau_{live}^k}}_{\text{mortality}} + \sum_j F_{jk} - \underbrace{(1 - \gamma^k) \frac{C_{b_dead}^k}{\tau_{dead}^k} - \gamma^k \frac{C_{b_dead}^k}{\tau_{dead}^k}}_{\text{decomposition}}$$

$$\sum_k \gamma^k \frac{C_{b_dead}^k}{\tau_{dead}^k} = F_{ba}$$